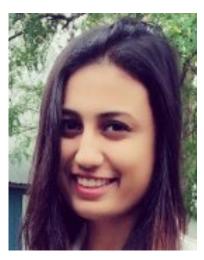
# Light-Supervision of **Structured Prediction Energy Networks**

#### **Andrew McCallum**

**Pedram** Rooshenas **Oregon PhD→UMass Postdoc** 



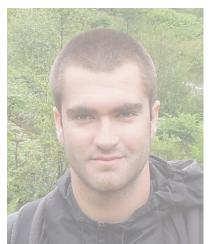
**Aishwarya Kamath UMass MS** 



SPENs [2016]

Generalized Expectation [Mann; Druck 2010-12] **David Belanger Greg Druck** 







# Light-Supervision

Prior Knowledge as Generalized Expectation

...induces extra structural dependencies...

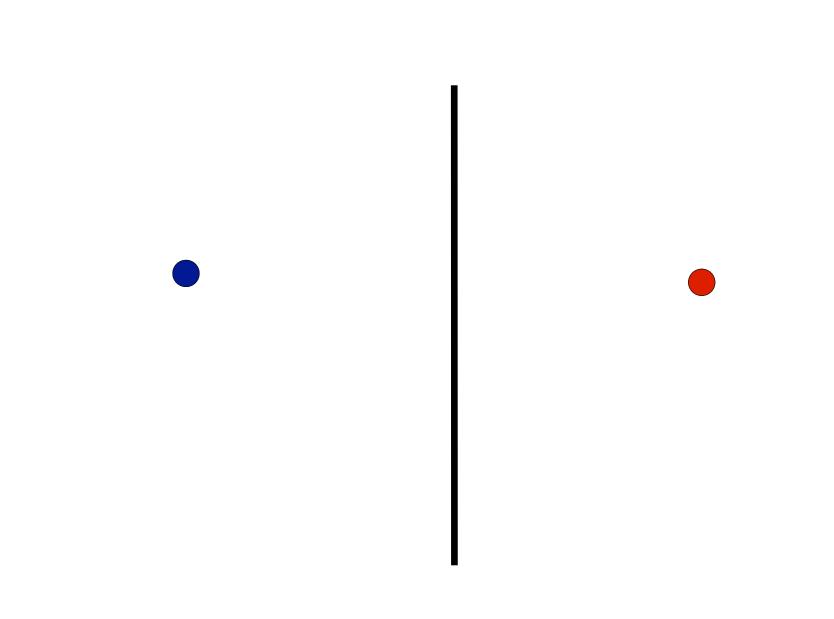
#### **Structured Prediction**

Complex dependencies with SPENs

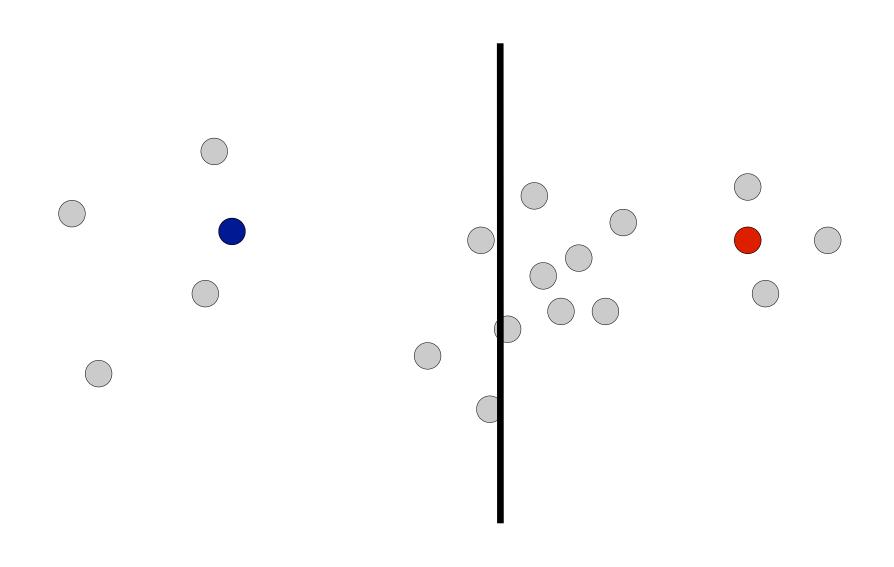
Chapter 1

## Generalized Expectation

### Learning from small labeled data

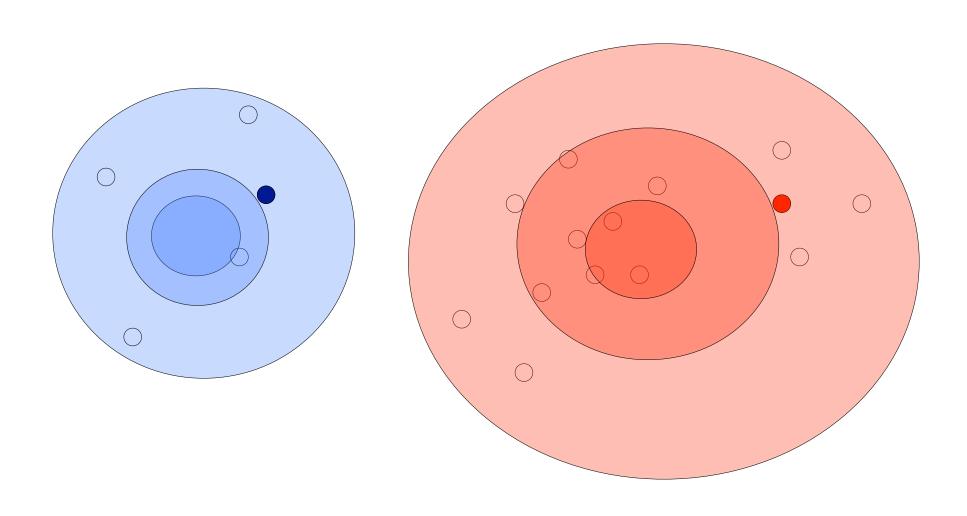


## Leverage unlabeled data



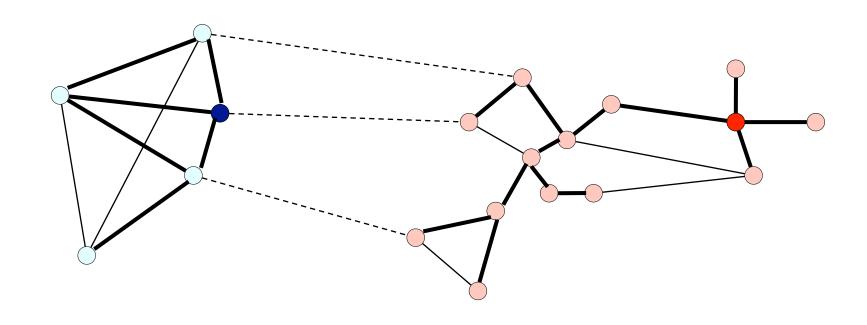
#### Family 1: Expectation Maximization

[Dempster, Laird, Rubin, 1977]



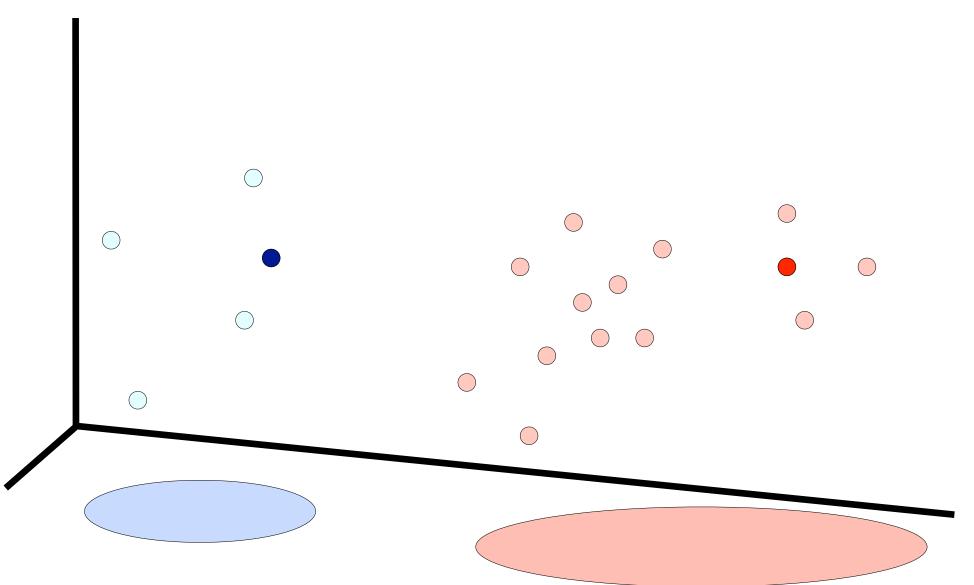
### Family 2: Graph-Based Methods

[Szummer, Jaakkola, 2002] [Zhu, Ghahramani, 2002]



### Family 3: Auxiliary-Task Methods

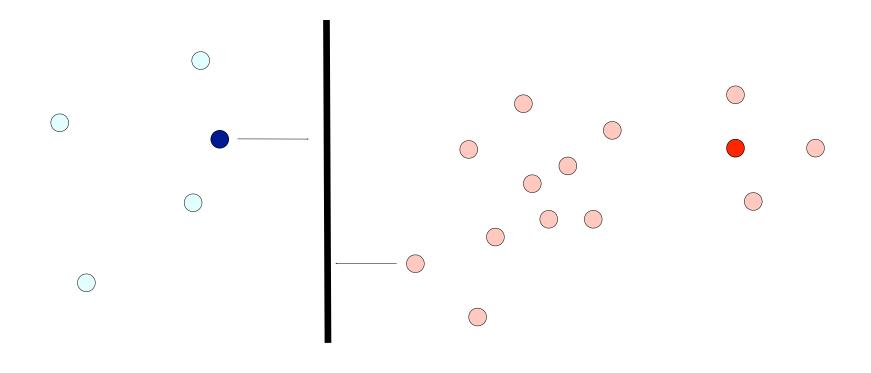
[Ando and Zhang, 2005]



#### Family 4: Boundary in Sparse Region

Transductive SVMs [Joachims, 1999]: Sparsity measured by margin

Entropy Regularization [Grandvalet & Bengio, 2005]: minimize label entropy



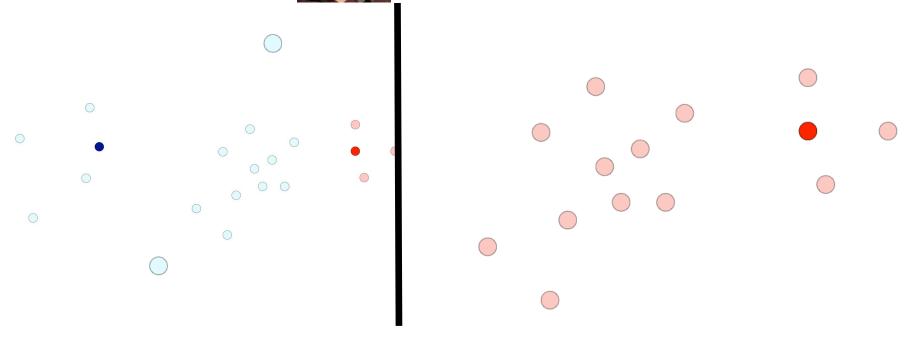
#### Family54 GBoera bland Experimen Reigion

[Mann, Mracoaldunctive 180/10/su[choaldrainms, Meea]/Loop and the information 2]

Entropy Regularization

Ivalet & Bengio, 2005]: minimize label entropy

best solution?

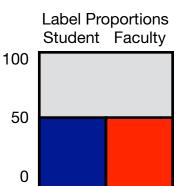


Label | Feature Expectations

E[p(y|f(x))]

Label Prior Expectations

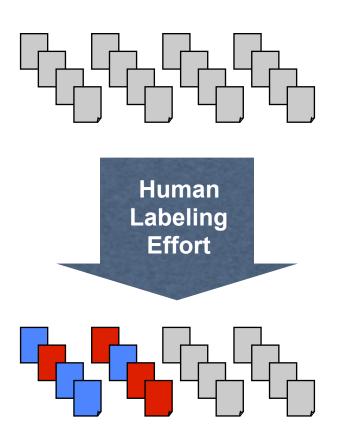
E[p(y)]



### **Expectations on Labels | Features**

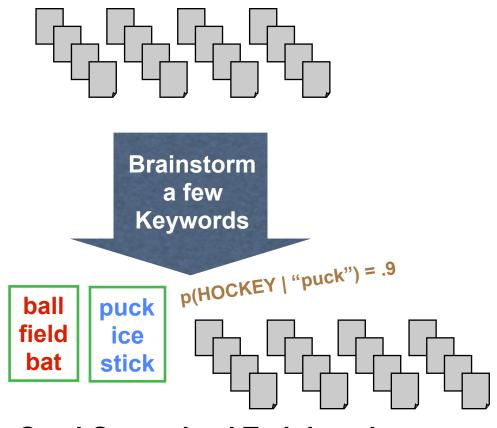
Classifying Baseball versus Hockey

#### **Traditional**



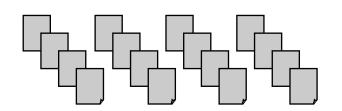
(Semi-)Supervised Training via
Maximum Likelihood

#### Generalized Expectation



Semi-Supervised Training via Generalized Expectation

### **Labeling Features**



~1000 unlabeled examples

features labeled . . .

hockey baseball HR Mets goal
Buffalo
Leafs
Toronto Maple
Leafs
puck
Lemieux

ball
Oilers Edmonton Oilers
Sox
Pens Pittsburgh
Penguins
runs

batting base NHL Bruins Penguins

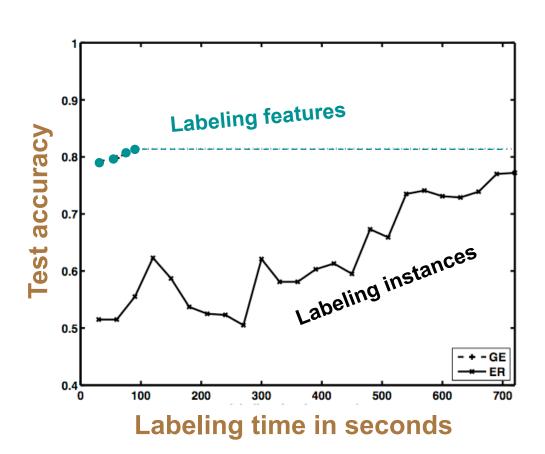
Accuracy 85%

92%

94.5%

96%

#### **Accuracy per Human Effort**



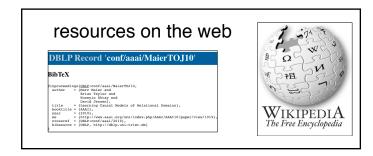
### Prior Knowledge

#### Feature labels from humans

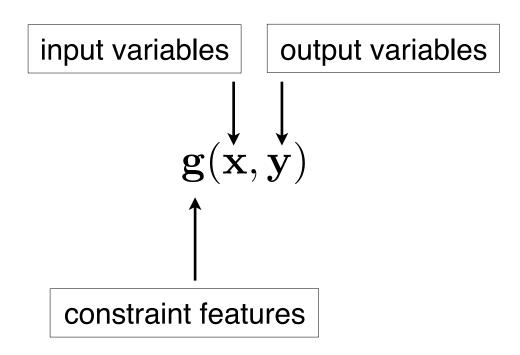
#### **baseball/hockey** classification

baseball	hockey
hit	puck
braves	goal
runs	nhl

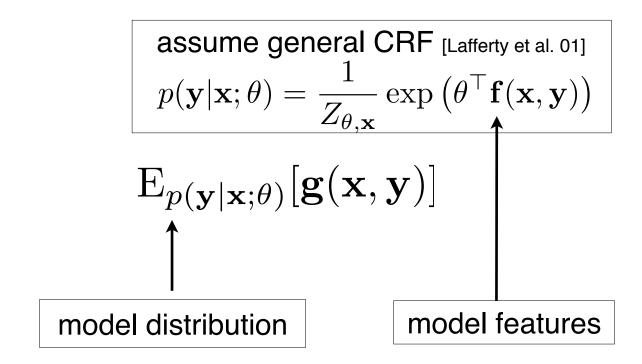
#### many other sources







returns 1 if x contains "hit" and y is baseball



model probability of **baseball** if **x** contains "hit"

$$\mathrm{E}_{\tilde{p}(\mathbf{x})}[\mathrm{E}_{p(\mathbf{y}|\mathbf{x};\theta)}[\mathbf{g}(\mathbf{x},\mathbf{y})]]$$

empirical distribution

(can be defined as)
model's probability that
documents that contain "hit" are labeled baseball

(soft) expectation constraint

$$S(\mathbf{E}_{\tilde{p}(\mathbf{x})}[\mathbf{E}_{p(\mathbf{y}|\mathbf{x};\theta)}[\mathbf{g}(\mathbf{x},\mathbf{y})]])$$

larger score if model expectation matches prior knowledge

score function

#### **Objective Function**

$$\mathcal{O}(\theta) = S(\mathbf{E}_{\tilde{p}(\mathbf{x})}[\mathbf{E}_{p(\mathbf{y}|\mathbf{x};\theta)}[\mathbf{g}(\mathbf{x},\mathbf{y})]]) + r(\theta)$$

$$\uparrow$$
regularization

#### **GE Score Functions**

$$\mathcal{O}(\theta) = S(\mathcal{E}_{\tilde{p}(\mathbf{x})}[\mathcal{E}_{p(\mathbf{y}|\mathbf{x};\theta)}[\mathbf{g}(\mathbf{x},\mathbf{y})]]) + r(\theta)$$

target expectations

model expectations

$$\mathbf{g}_{ heta} =$$

squared error: 
$$S_{l_2^2}(\theta) = - || \hat{\mathbf{g}} - \mathbf{g}_{\theta} ||_2^2$$

target expectations

model expectations

$$\hat{\mathbf{g}} = \left\{\begin{array}{c} \mathbf{\hat{g}} \\ \mathbf{\hat{g}} \end{array}\right\}$$
 "puck"  $\mathbf{\hat{g}}$  "hit"

$$\mathbf{g}_{ heta} =$$

KL divergence:  $S_{KL}(\theta) = -\sum \hat{\mathbf{g}}_q \log \frac{\hat{\mathbf{g}}_q}{\hat{\mathbf{g}}_q}$ 

### Estimating Parameters with GE

$$\mathcal{O}(\theta) = S(\mathcal{E}_{\tilde{p}(\mathbf{x})}[\mathcal{E}_{p(\mathbf{y}|\mathbf{x};\theta)}[\mathbf{g}(\mathbf{x},\mathbf{y})]]) + r(\theta)$$

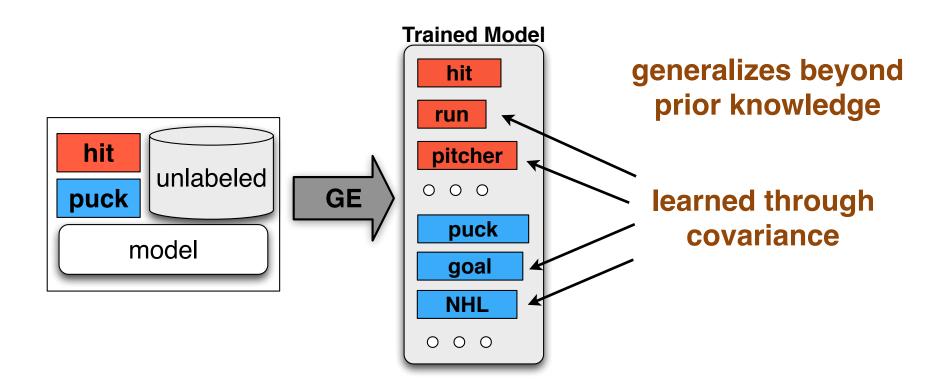
KL: 
$$v_i = \frac{g_i}{g_{\theta i}}$$

violation term: KL: 
$$v_i = \frac{\hat{g}_i}{g_{\theta i}}$$
 sq. error:  $v_i = -2(\hat{g}_i - g_{\theta i})$ 

$$\nabla_{\theta} \mathcal{O}(\theta) = \mathbf{v}^{\top} \Big( \mathbf{E}_{\tilde{p}(\mathbf{x})} [\mathbf{E}_{p(\mathbf{y}|\mathbf{x};\theta)} [\mathbf{g}(\mathbf{x}, \mathbf{y}) \mathbf{f}(\mathbf{x}, \mathbf{y})^{\top}] \\ - \mathbf{E}_{p(\mathbf{y}|\mathbf{x};\theta)} [\mathbf{g}(\mathbf{x}, \mathbf{y})] \mathbf{E}_{p(\mathbf{y}|\mathbf{x};\theta)} [\mathbf{f}(\mathbf{x}, \mathbf{y})^{\top}] \Big) + \nabla_{\theta} r(\theta)$$

estimated covariance between model and constraint features

#### **Learning About Unconstrained Features**



#### Generalized Expectation criteria

#### Easy communication with domain experts

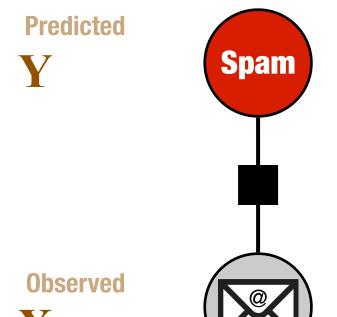
- Inject domain knowledge into parameter estimation
- Like "informative prior"...
- ...but rather than the "language of parameters" (difficult for humans to understand)
- ...use the "language of expectations" (natural for humans)

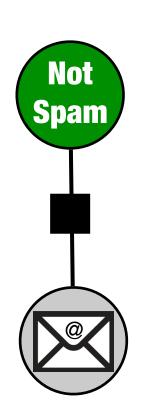
#### **IID Prediction**

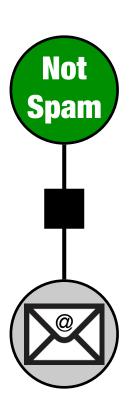
"classification" e.g. logistic regression

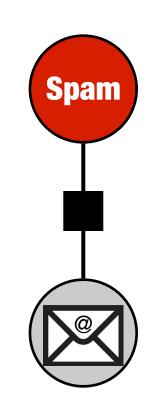
Example: Spam Filtering





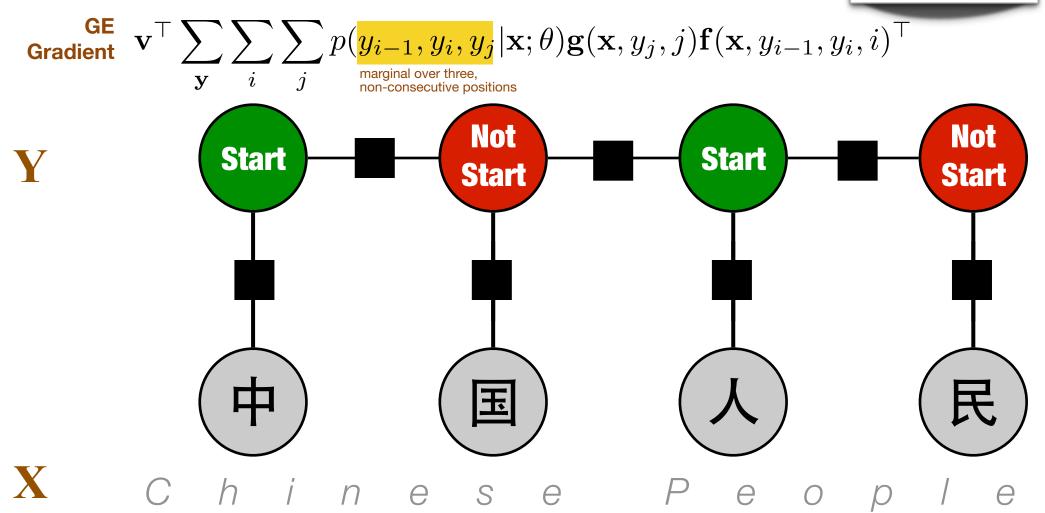






e.g. "sequence labeling" Chinese Word Segmentation

$$\mathcal{O}(\theta) = S(\mathbf{E}_{\tilde{p}(\mathbf{x})}[\mathbf{E}_{p(\mathbf{y}|\mathbf{x};\theta)}[\mathbf{g}(\mathbf{x},\mathbf{y})]]) + r(\theta)$$
Linear-chain CRF



# **Natural Expectations** lead to Difficult Training Inference

"AUTHOR field should be contiguous, only appearing once."

Anna Popescu (2004), "Interactive Clustering,"

Wei Li (Ed.), Learning Handbook, Athos Press,

Souroti.

 $p(y_{i-1}, y_i, y_i, y_k)$ 

The downfall of GE.



A framework providing easier inference for complex dependencies?

#### Structured Prediction Energy Networks

Deep Learning

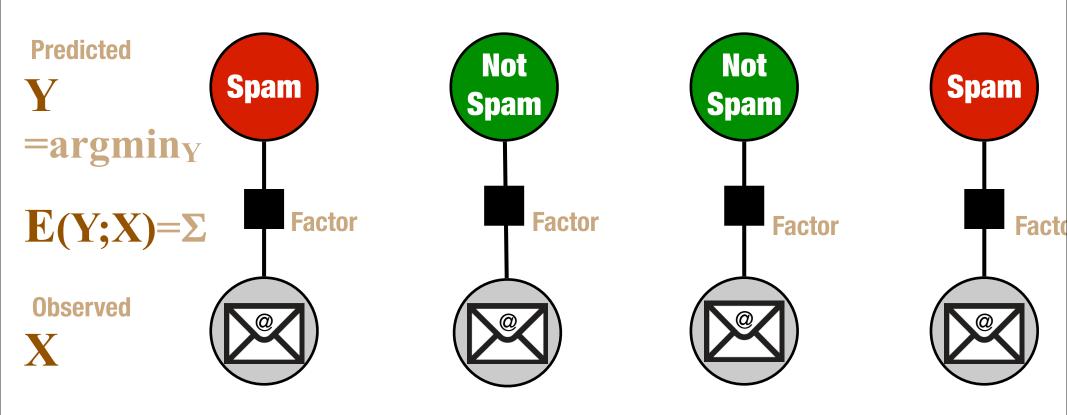
+

Structured Prediction

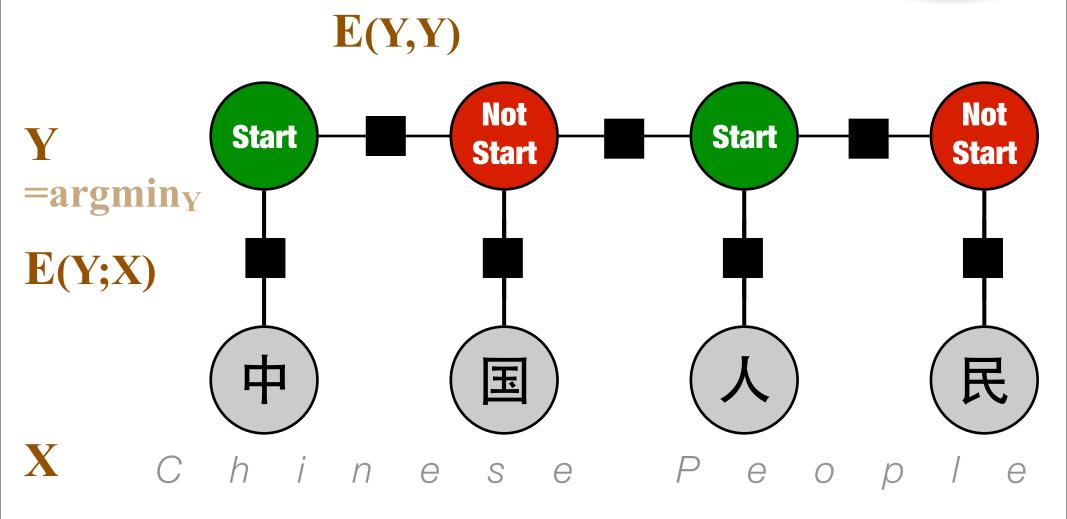
"classification" e.g. logistic regression

**Example: Spam Filtering** 

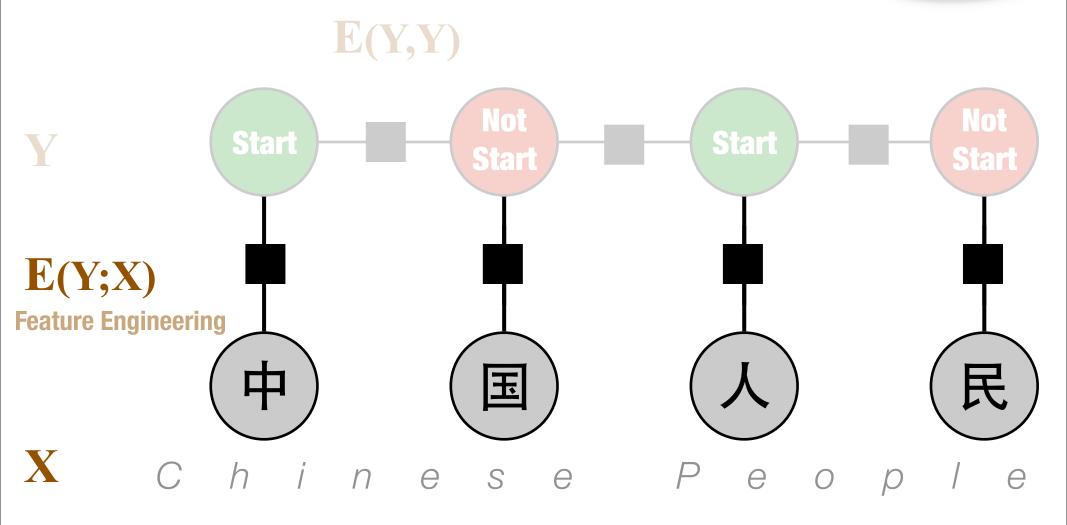




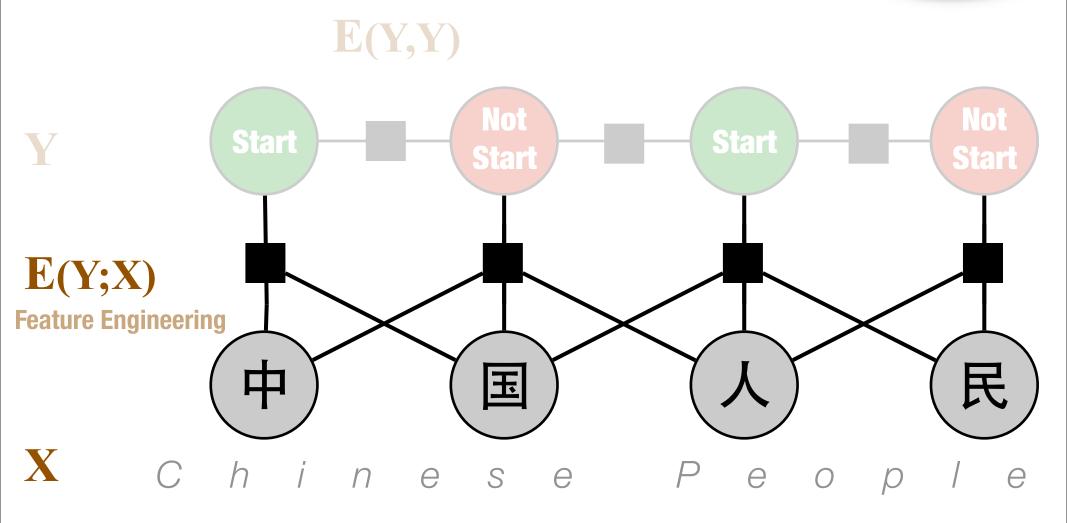
e.g. "sequence labeling"



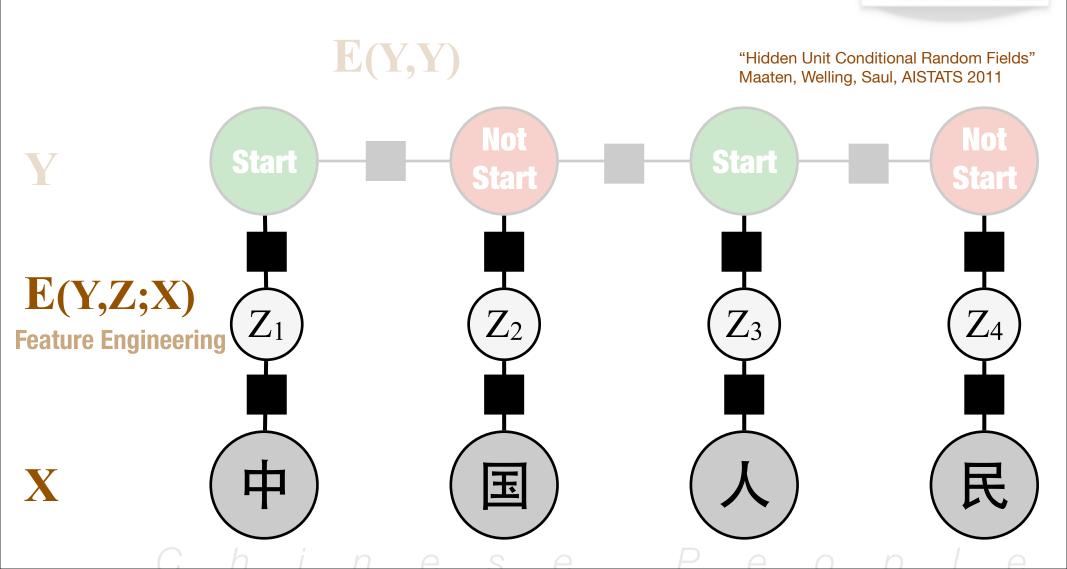
e.g. "sequence labeling"



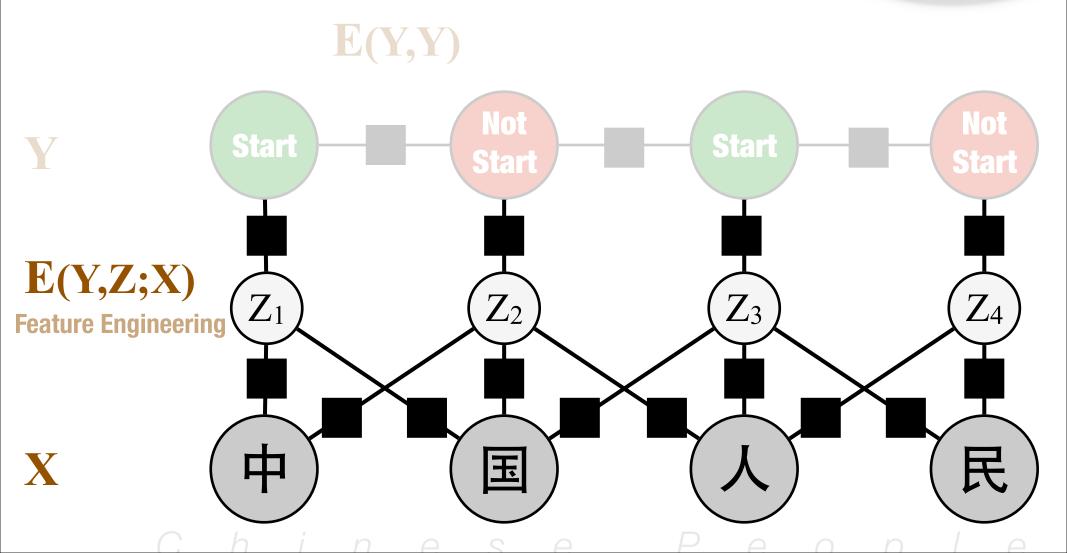
e.g. "sequence labeling"



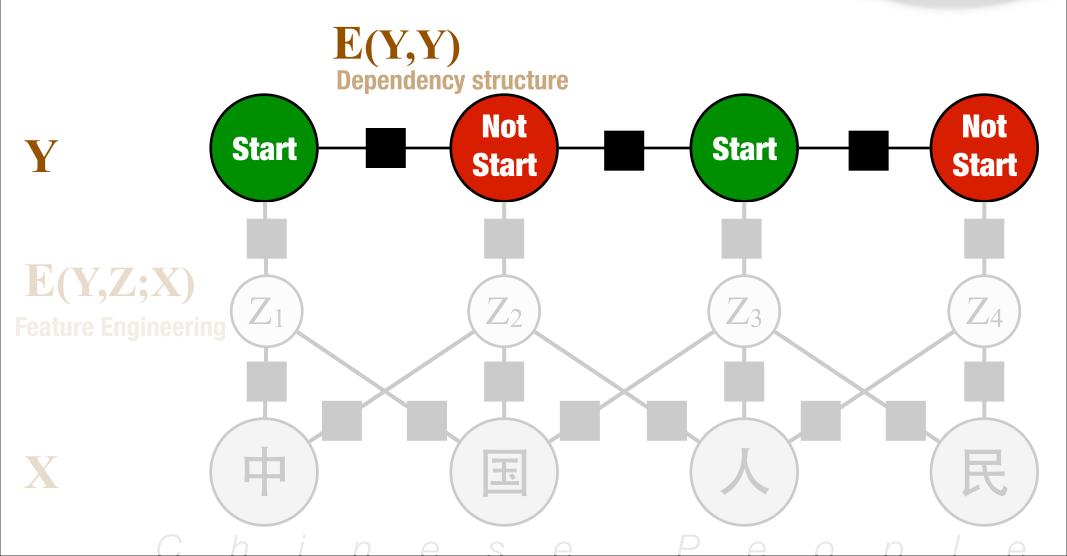
e.g. "sequence labeling"



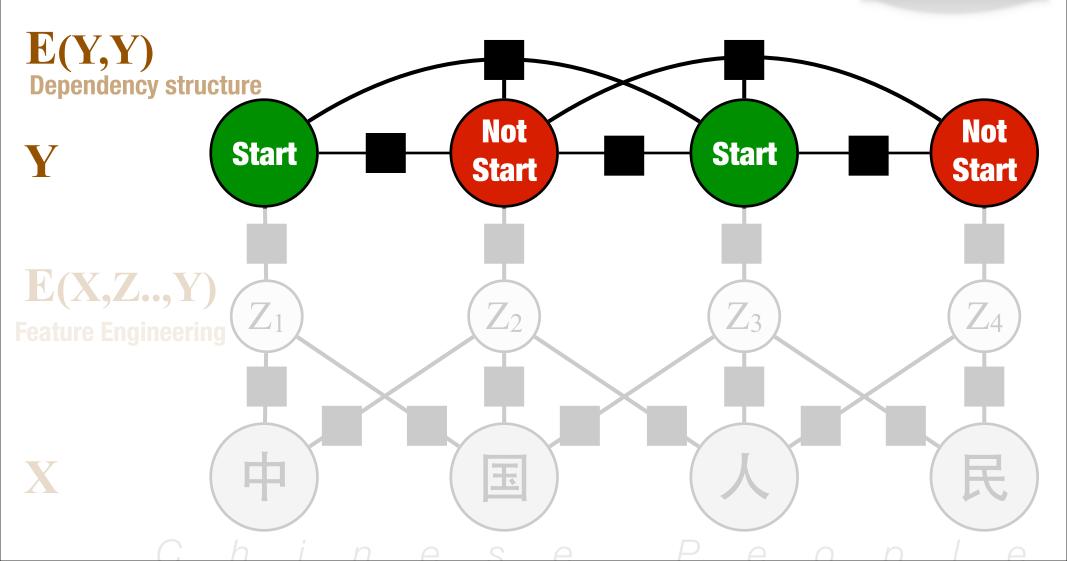
e.g. "sequence labeling"



e.g. "sequence labeling"

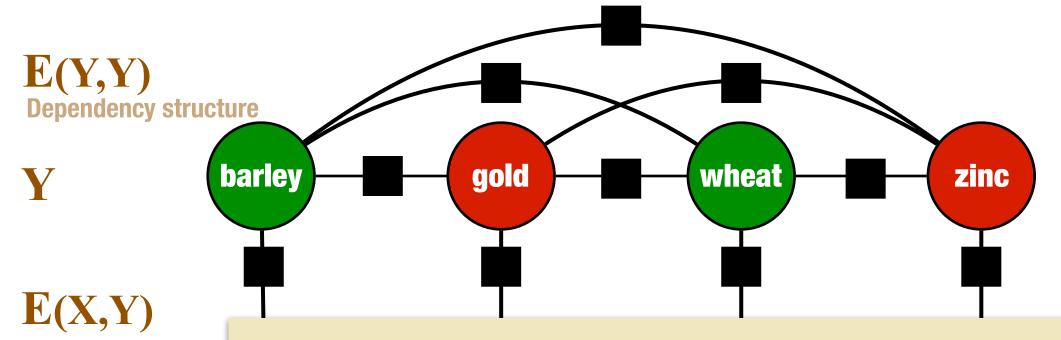


e.g. "sequence labeling"

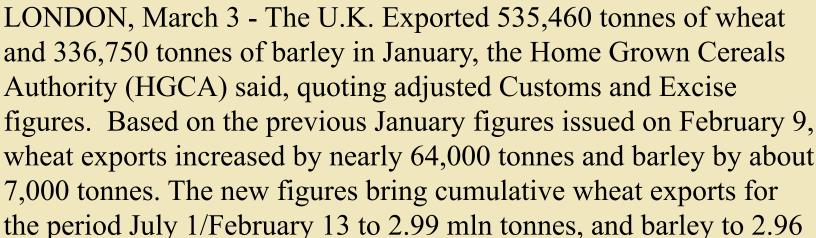


e.g. "multi-label classification"

Example: Multi-label Document Classification



**Feature Engineering** 

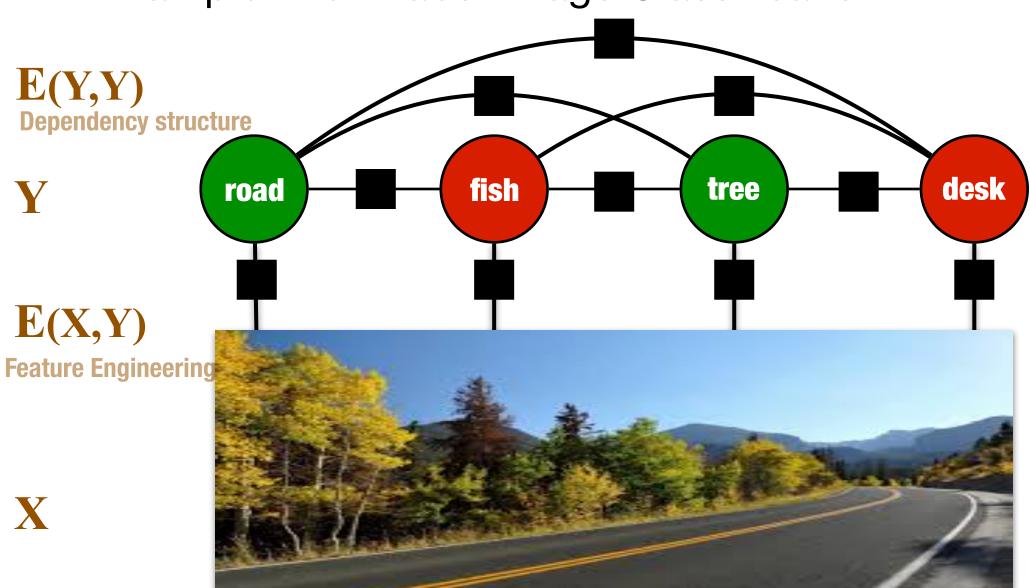




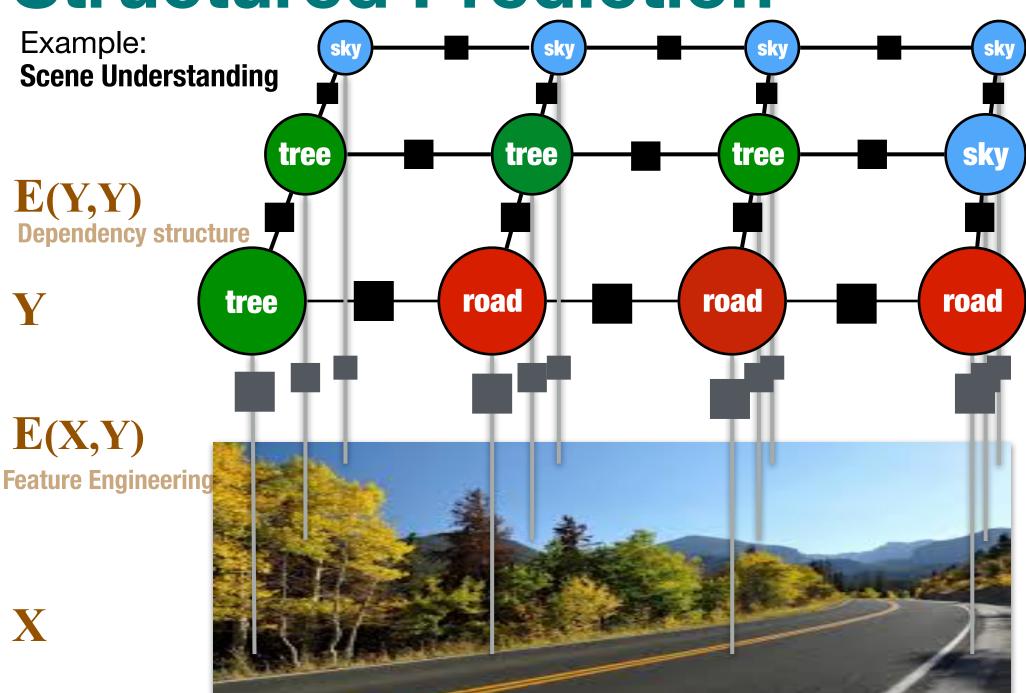
### **Structured Prediction**

e.g. "multi-label classification"

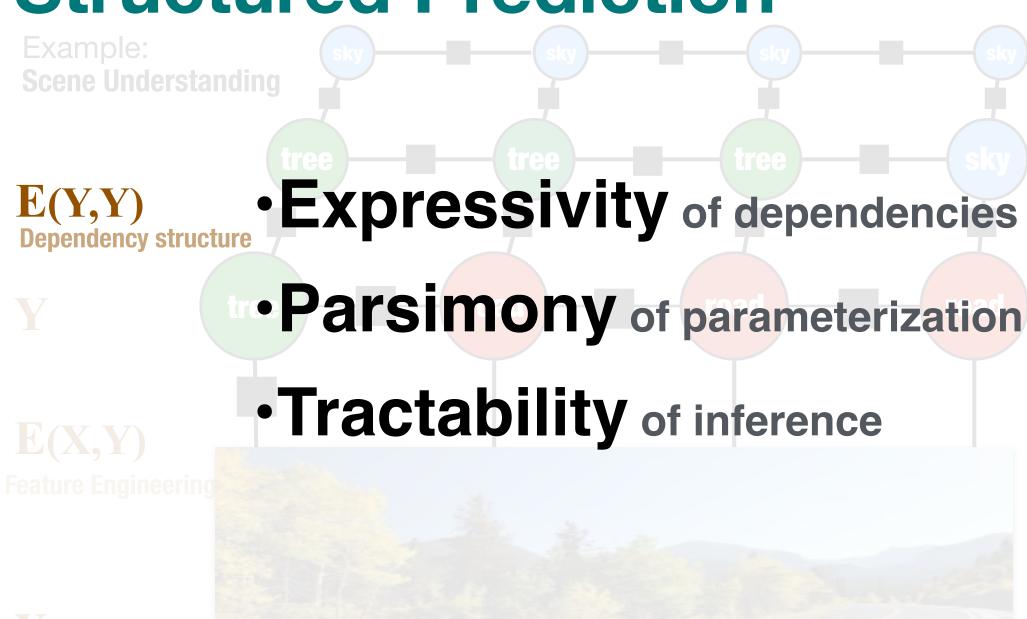
Example: Multi-label Image Classification

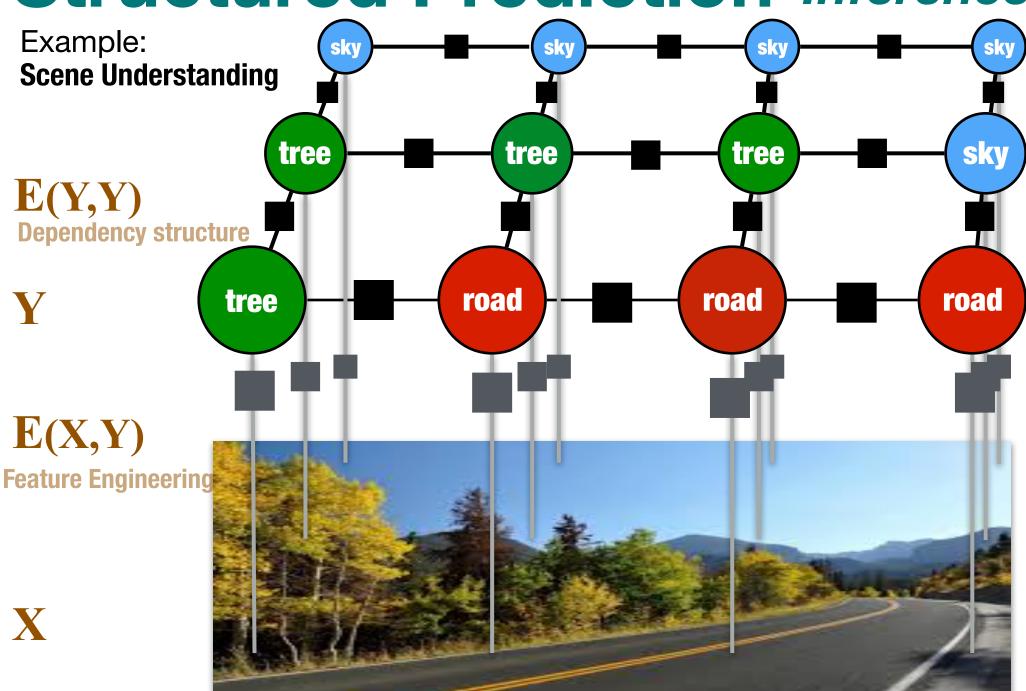


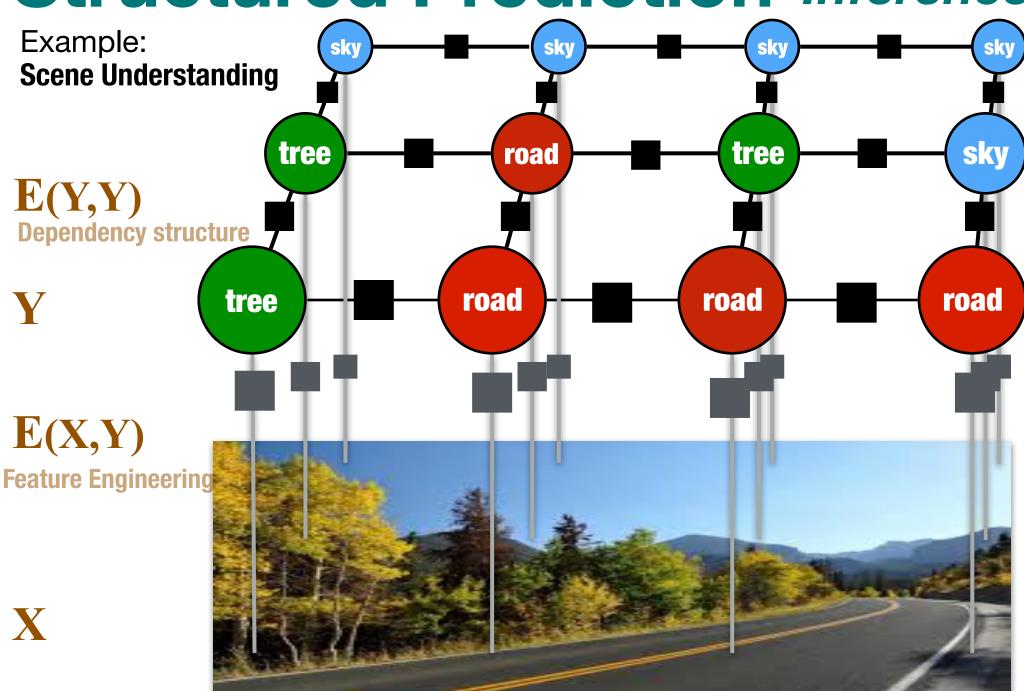
## **Structured Prediction**

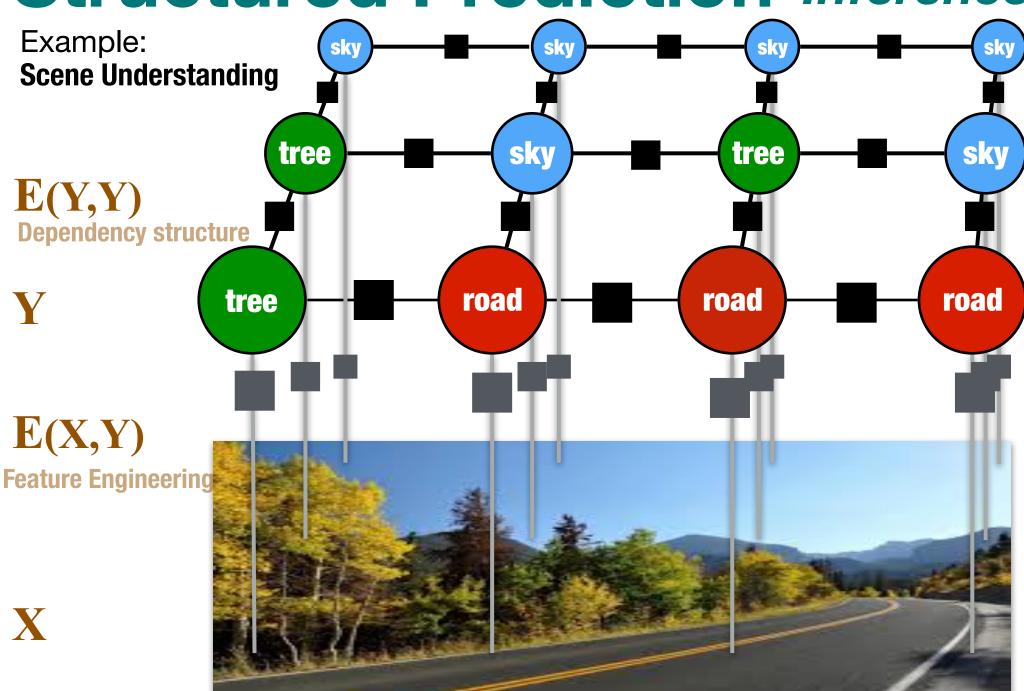


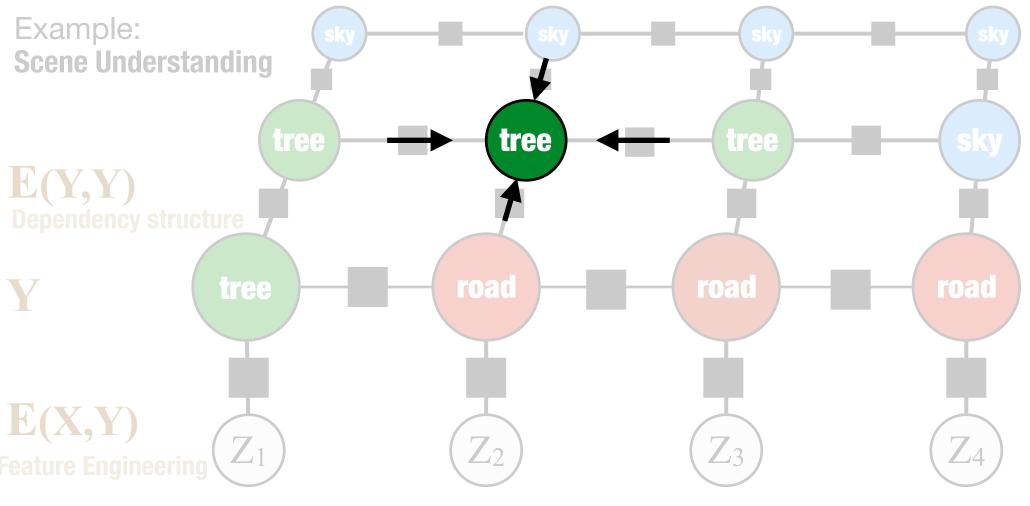
## **Structured Prediction**









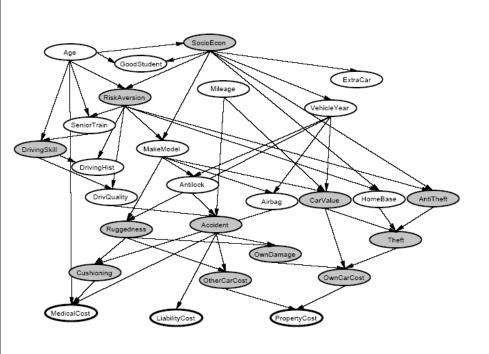


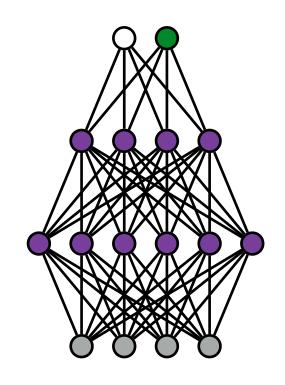
$$m_{i \to j}^{(t+1)}(x_j) = \sum_{x_i} \Phi_{ij}(x_i, x_j) \Phi_i(x_i) \prod_{k \in N(i)} m_{k \to i}^{(t)}(x_i)$$



# **Bayesian Network**

## Deep Learning





Sparsely connected
Hand-designed representations
Loopy/iterated inference (typically)
Cautious about capacity
"Statistically conscientious"

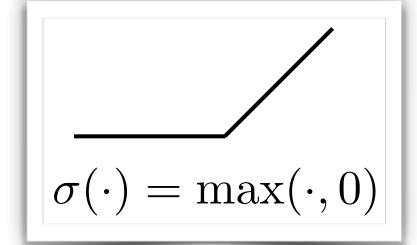
Densely connected (learn connectivity)
Learned, distributed representations
Feed-forward inference (typically)
Wild about high capacity
"Wild West"

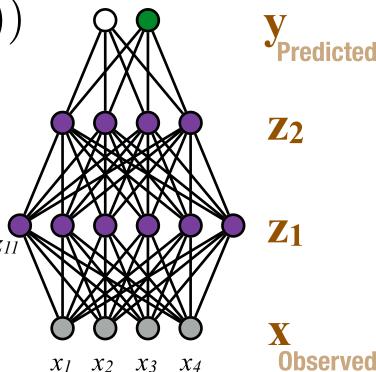
## **Deep Learning**

$$\mathbf{y} = \sigma \left( \mathbf{y} V_{\overline{3}} \mathbf{z} \mathbf{g} \right) \left( W_3 \sigma \left( W_2 \sigma \left( W_1 \mathbf{x} \right) \right) \right)$$

$$\mathbf{z}_2 = \sigma\left(W_2\mathbf{z_1}\right)$$

$$z_{11} = \sigma \left( \sum_{i} \mathbf{z}_{1} w_{T1} \sigma c(W_{1}\mathbf{x}) \right)_{z_{ii}}$$





## Deep Learning

$$\mathbf{y} = F\left(\mathbf{x}; W\right)$$

Training Data 
$$\left\{\mathbf{x}^{(i)},\mathbf{y}^{(i)}
ight\}_{i=1}^{N}$$

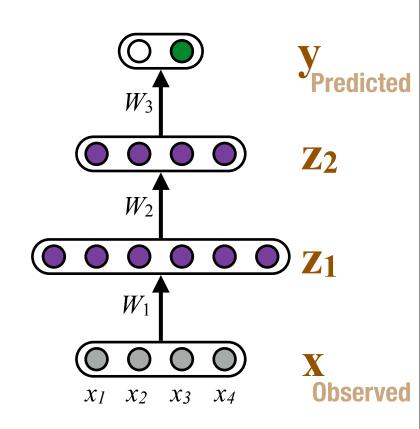
#### Loss

$$\mathcal{L} = \sum_i L\left(F(\mathbf{x^{(i)}}; W), \mathbf{y^{(i)}}\right)$$
 e.g. Squared error, Cross-entropy,...

#### **Training**

$$\mathop{
m arg\ min}_{W} \mathcal{L}$$
 Gradient descent

$$W_{\text{new}} = W_{\text{old}} - \alpha \frac{\partial \mathcal{L}(W)}{\partial W}$$

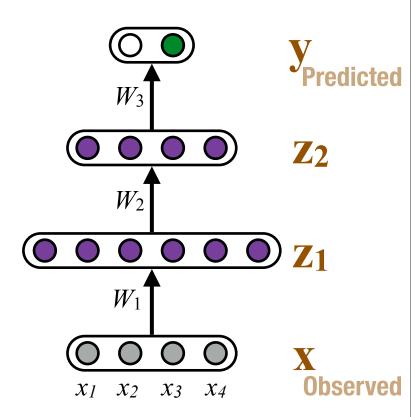


#### **Key tools:**

- (1) Back-propagation
- (2) Stochastic gradient descent

## Deep Learning

$$\mathbf{y} = F(\mathbf{x}; W)$$



#### **Back-propagation**

## **Deep Learning**

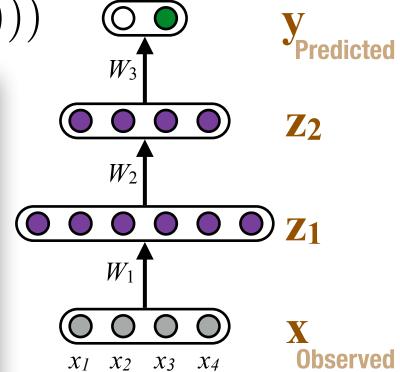
$$\mathbf{y} = \sigma \left( W_3 \sigma \left( W_2 \sigma \left( W_1 \mathbf{x} \right) \right) \right)$$

#### The "chain rule"

$$g(f(x))' = g'(f(x)) \cdot f'(x)$$

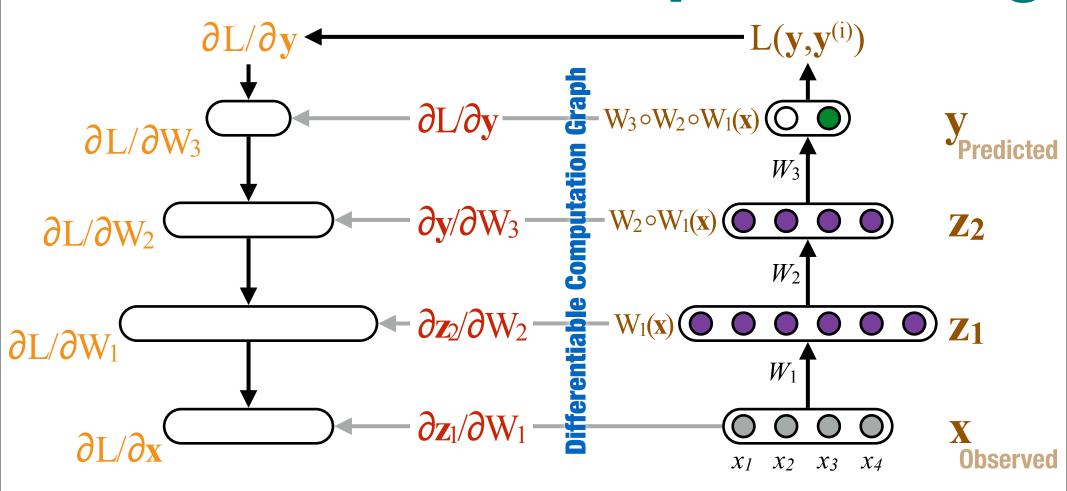
$$\frac{\partial g \circ f}{\partial x} = \frac{\partial g}{\partial f} \cdot \frac{\partial f}{\partial x}$$

$$\frac{\partial j \circ i \circ h \circ g \circ f}{\partial x} = \frac{\partial j}{\partial i} \frac{\partial i}{\partial h} \frac{\partial h}{\partial g} \frac{\partial g}{\partial f} \frac{\partial f}{\partial x}$$



#### **Back-propagation**

## **Deep Learning**

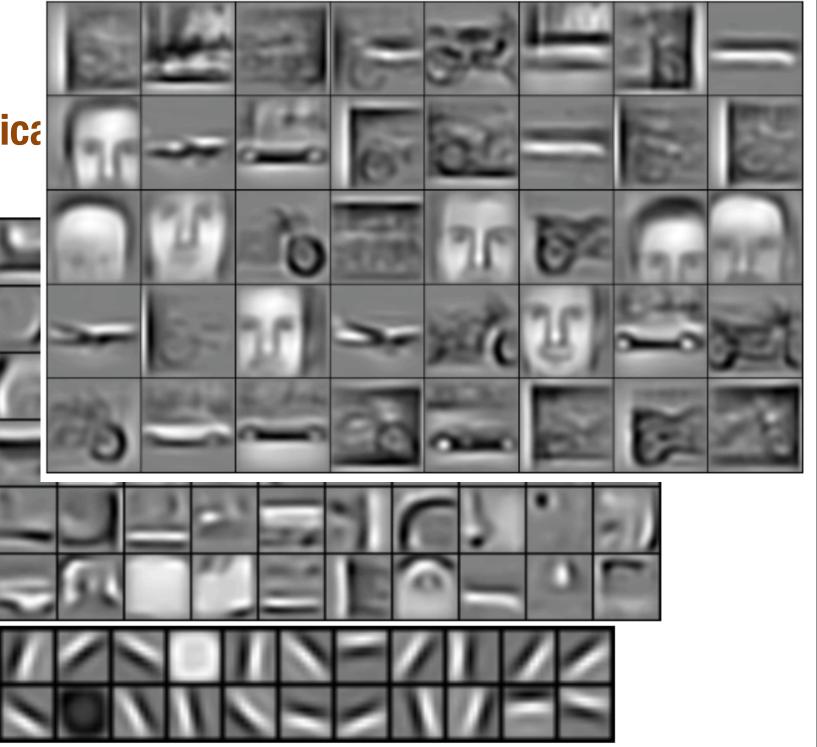


Can get gradient of Loss wrt parameters at any depth from

- (1) local partial derivative functions
- (2) numeric gradient from above

Example:
CNNs for
Object Classifica
in Images

Representation Learning



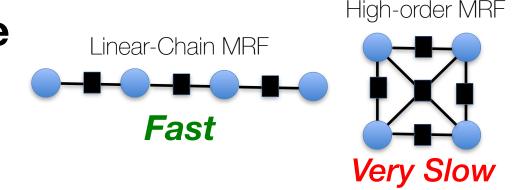
### **Motivation for SPENs**

Use power of

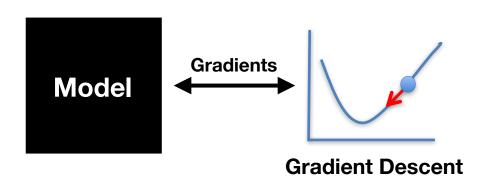
1. deep learning for structure learning

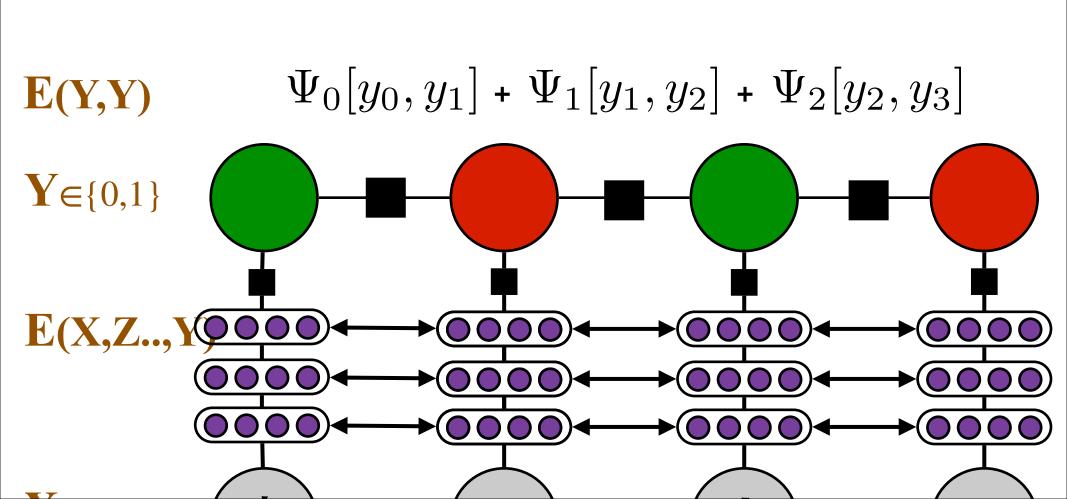


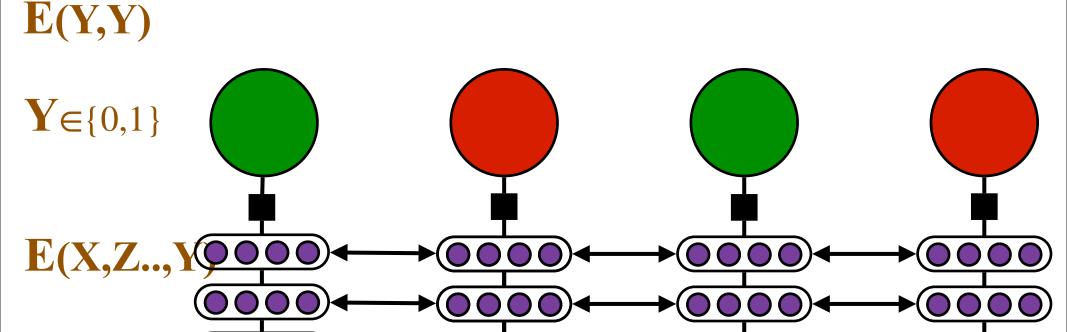
2. Provide an alternative to graphical models.

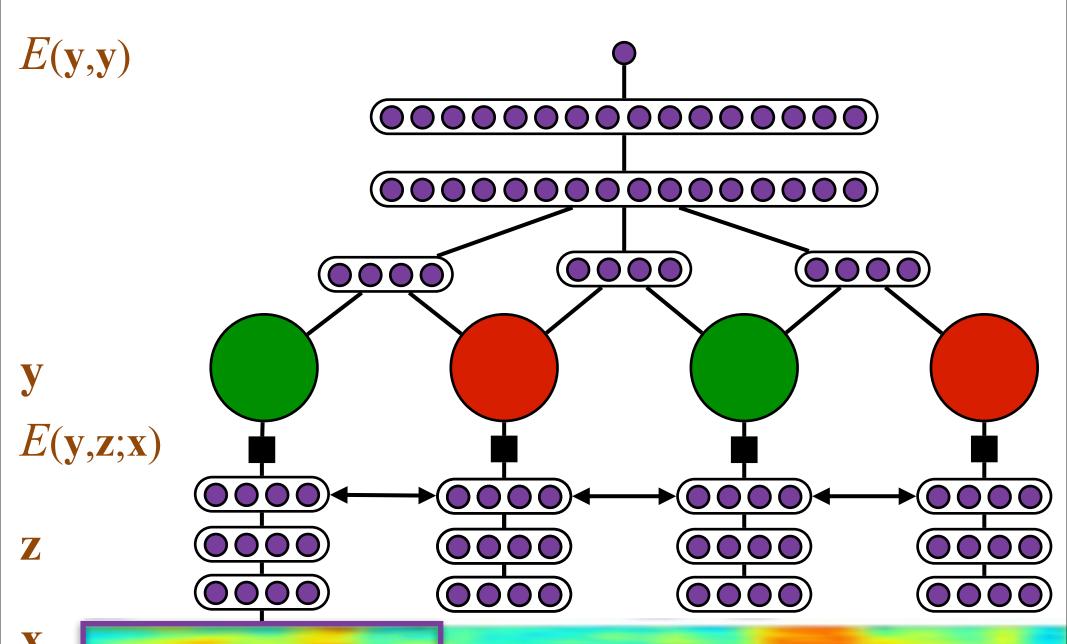


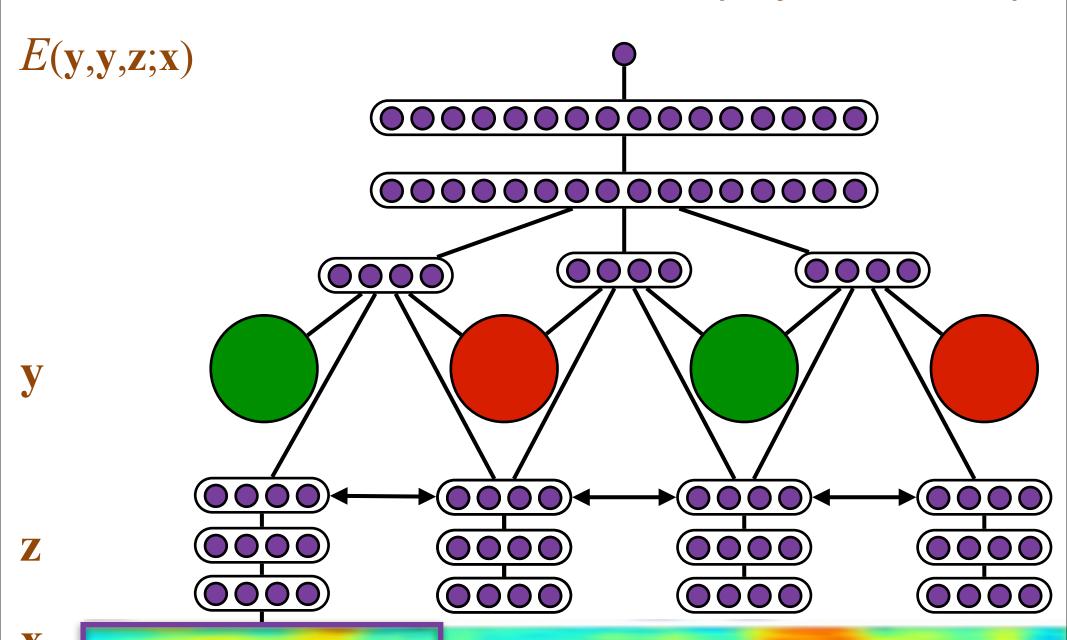
3. Black-box interaction with model.











[Belanger, McCallum, ICML 2016]

**Energy network** 

$$E(\bar{\mathbf{y}}; F(\mathbf{x}))$$

Soft prediction... found by gradient descent

$$\bar{\mathbf{y}}^* = \arg\min_{\bar{\mathbf{y}} \in [0,1]^L} E(\bar{\mathbf{y}}; F(\mathbf{x}))$$

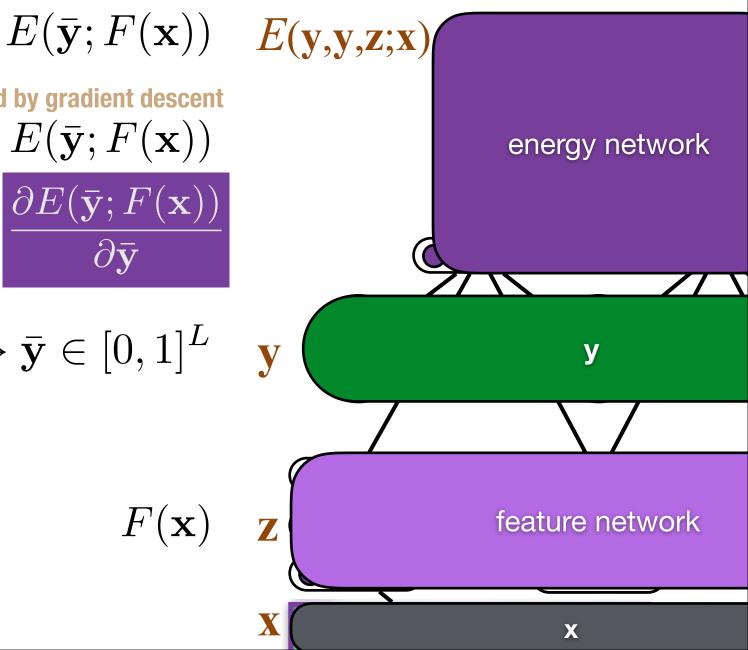
$$\frac{\partial E(\bar{\mathbf{y}}; F(\mathbf{x}))}{\partial E(\bar{\mathbf{y}}; F(\mathbf{x}))}$$

Relax y, to be continuous

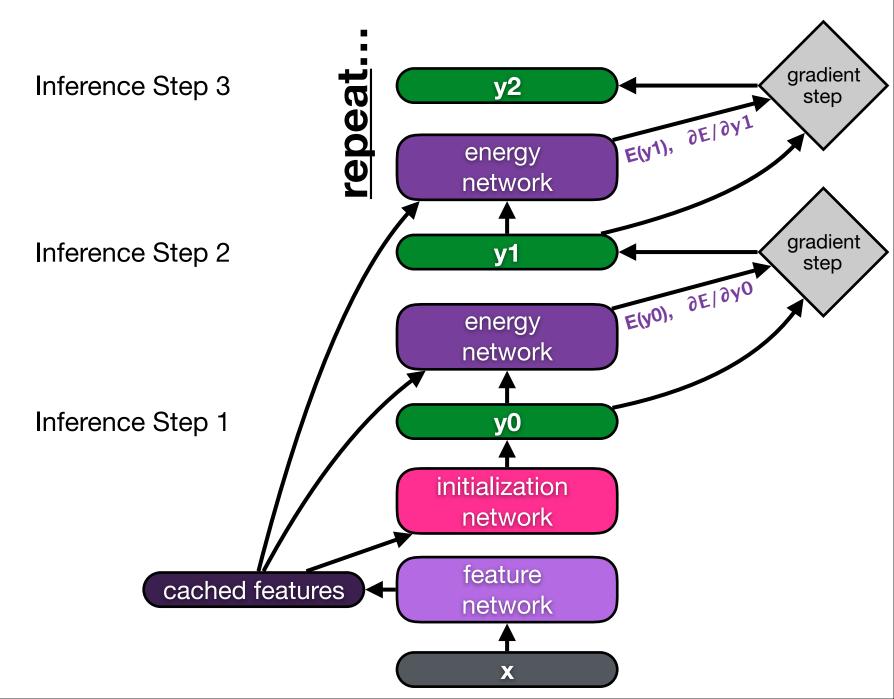
$$\mathbf{y} \in \{0,1\}^L \to \bar{\mathbf{y}} \in [0,1]^L$$

**Feature Network** 

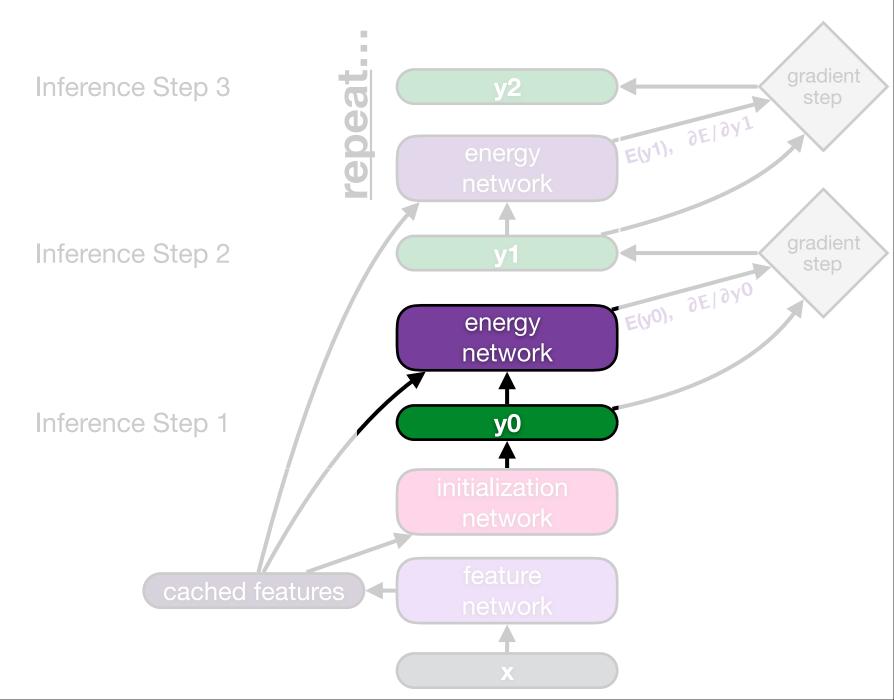
$$F(\mathbf{x})$$



## **SPEN Inference Graph**



### **SPEN Inference Graph**



#### **Gradient used to Modify Inputs**

"A Neural Algorithm for Artistic Style" [Gatys et al. 2015]





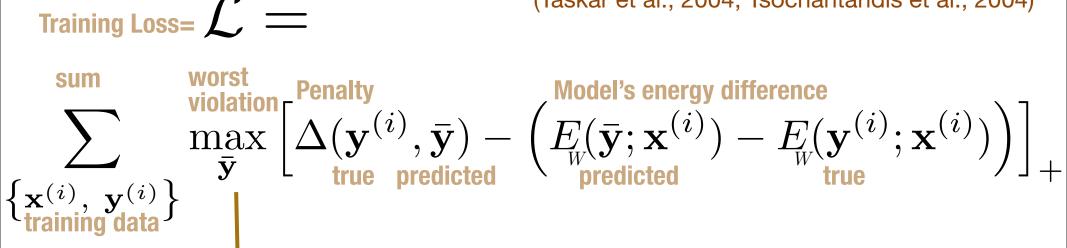
SPENs use similar idea:

Optimize energy using backprop all the way down to the raw pixels.

### **Learning Algorithm 1:** Structured SVM

Training Loss= 
$$\mathcal{L}$$
 =

(Taskar et al., 2004; Tsochantaridis et al., 2004)



search requires Loss-Augmented Inference

$$\arg\min_{\bar{\mathbf{y}}} \left( -\Delta(\mathbf{y}^{(i)}, \bar{\mathbf{y}}) + E_{_{W}}(\bar{\mathbf{y}}; \mathbf{x}^{(i)}) \right)$$
Penalty must be differentiable

**Stochastic Gradient** 

$$\frac{\partial \mathcal{L}}{\partial W}$$

### **Learning Algorithm 2:**

#### End-to-end "backprop through inference"

Training Loss= 
$$\mathcal{L} =$$

Direct Risk Minimization

$$\sum_{i} L\left(\mathbf{y}^{(ii)}, \mathbf{Algorith}_{\mathbf{y}}(\mathbf{x}^{(i)})\right)$$

training data

Direct application of: Justin Domke, AISTATS, 2012.

"Generic Methods for Optimization-Based Modeling"

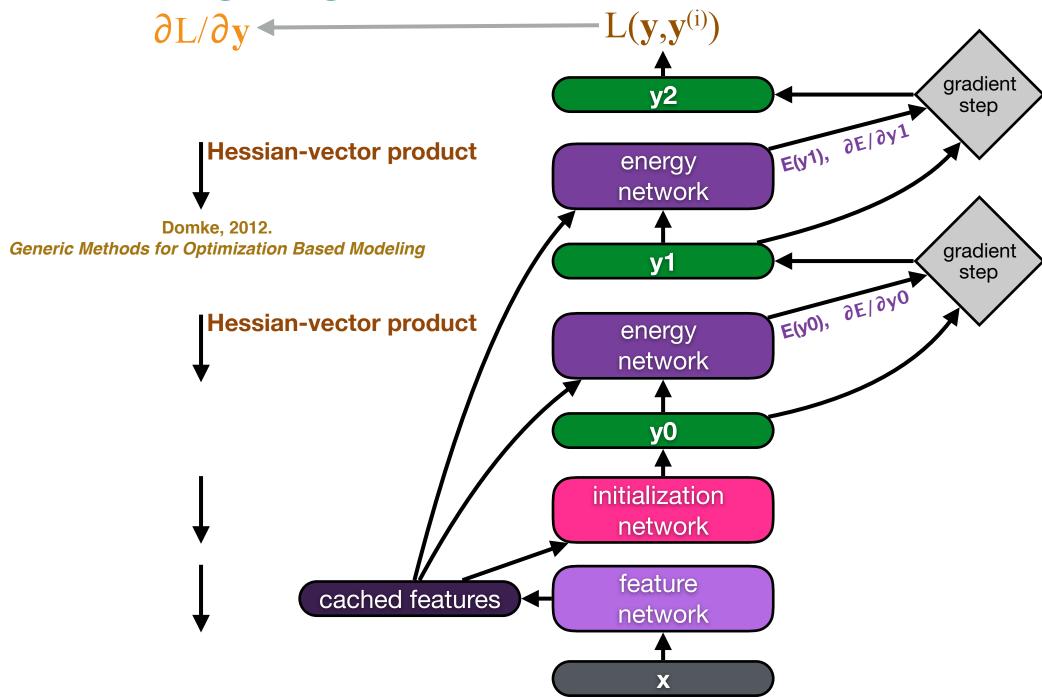
Algorithm for inference 
$$ar{f y}^*=ar{f y}^{[0]}+\sum_{t=1}^T lpha_t rac{\partial}{\partial ar{f y}} E_W({f x},ar{f y}^{[t-1]})$$

sum over "time steps" of inference

$$\frac{\partial \mathcal{L}}{\partial W} = \frac{\partial L}{\partial \bar{\mathbf{y}}^*} \frac{\partial \bar{\mathbf{y}}^*}{\partial W} = \sum_{t=1}^T \alpha_t \frac{\partial L}{\partial \bar{\mathbf{y}}^*} \left( \frac{\partial}{\partial W} \frac{\partial}{\partial \mathbf{y}} E_W(\mathbf{x}, \bar{\mathbf{y}}^{[t-1]}) \right)$$
Hessian-Vector product can be approximated using one-dimensional finite differences.

sum over "time steps" of inference

### **Learning Algorithm 2 Graph**





#### Light Supervision training of Structured Prediction Energy Networks

(Turing complete!)

- 1. Human writes arbitrary prior knowledge (SPEN)
- 2. Learn model with arbitrary dependencies.
- 3. Efficient inference by gradient descent.

Anna Popescu (2004), "Interactive Clustering," Wei Li (Ed.), Learning Handbook, Athos Press, Souroti.

#### Human writes arbitrary prior knowledge...

"AUTHOR field should be contiguous, only appearing once."

#### ...as a scoring function V(x=citation, y=labeling)

```
score = 0
score -= 1 foreach AUTHOR non-contiguous
score -= 1 if has both JOURNAL & BOOKTITLE
score -= 1 foreach "using" not in TITLE
score -= 1 foreach [A-Z]\. not AUTHOR|EDITOR
score -= 1 if PUBLISHER before JOURNAL ...
```

(like rule-based AI before ML was popular)

## Why use ML if we get a ruled-based scoring function?

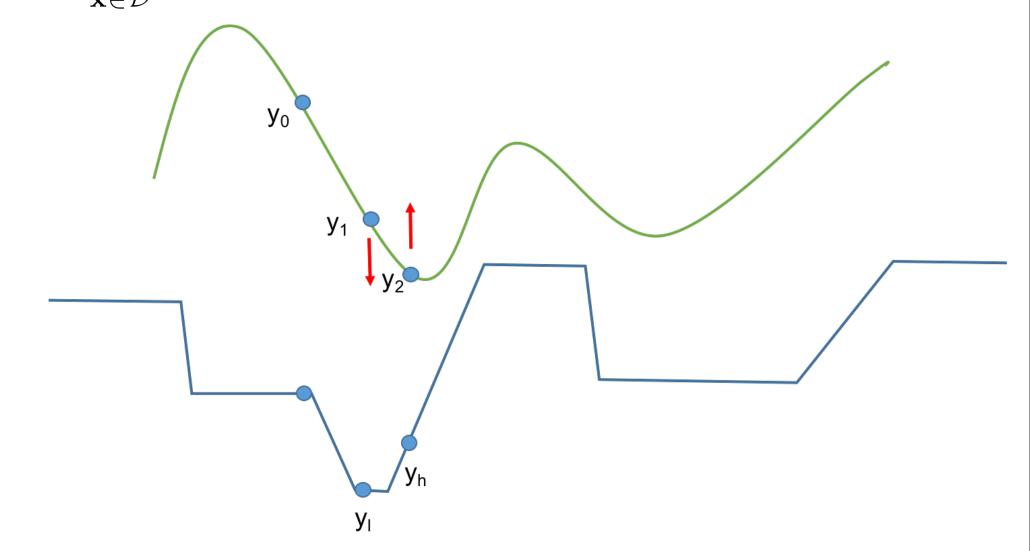
- Doesn't generalize
  - examines just a few features
  - SPENs will learn correlated features, labels.

- No inference procedure just scores for given (x,y)
  - stochastic optimization is slow
  - SPENs provide gradient-descent inference

### **Learning Algorithm 3:**

#### "ranking successive gradient steps"

$$\sum_{\mathbf{x} \in \mathcal{D}} [\alpha(V(\mathbf{y}_h, \mathbf{x}) - V(\mathbf{y}_l, \mathbf{x})) - E_{\mathbf{w}}(\mathbf{y}_h, \mathbf{x}) + E_{\mathbf{w}}(\mathbf{y}_l, \mathbf{x})]_{+}$$



## **Preliminary Experiments**

(...much more work and comparisons in future...)

## Weak-Sup SPEN: simple test Multi-label Document Classification

#### x = Medical bag-of-words

[amount, cystourethrogram, diagnosed, episode, evaluate, exam, fever, grade, growth, hematuria, infection, interval, kidney, left, lower, occurred, patient, pole, previously, purpose, reflux, renal, scar, scarring, small, study, tract, urinary, vesicoureteral, voiding, year]

y = multiple ICM-9-CD codes

[593-70, 599-00]

#### x = Human background knowledge

Keyword descriptions of ICM-9-CD codes. (Not gathering any labeled correlation knowledge.)

593-70: vesicoureteral, reflux, unspecified, nephropathy

V79-99: viral, chlamydial, infection, conditions, unspecified

753-00: renal, agenesis, dysgenesis

#### Scoring function gives +1 for each label:keyword cooccurrence.

$$V(y^i,x^i) = \sum_j I(l_j \in y^i) I(|x^i \cap w_j| > 0) - \gamma \max(|y^i| - 1,0)$$
 Label, Keyword matches Sparsity constraint

## Does the SPEN generalize over the human scoring function?

ICM-9-CD code data set, evaluate F1 of label set

Human Scoring Function, Exhaustive Search						
N≦1	N≦2	N≦3	N≦4	N≦5	N≦6	
15.5	18.3	19.6	20.5	21.1	20.3	22.6

(~10x faster)

## Weak-Sup SPEN: better test Citation Field Extraction

#### x = Citation Token Sequence

Anna Popescu (2004), "Interactive Clustering," Wei Li (Ed.), Learning Handbook, Athos Press, Souroti.

**y** = **Seq.** of **Labels** ∈ **|14|** 

AUTHOR AUTHOR YEAR TITLE TITLE
EDITOR, EDITOR EDITOR BOOKTITLE, BOOKTITLE
PUBLISHER PUBLISHER LOCATION

#### x = Human background knowledge

Human-written scoring function. 50 lines of code. Written in ~1 hour.

```
score -= 1 foreach AUTHOR non-contiguous
score -= 1 if has both JOURNAL & BOOKTITLE
score -= 1 foreach "using" not in TITLE
...
```

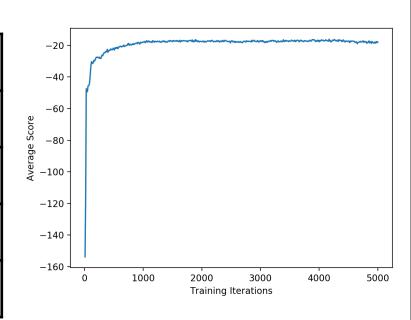
~4000 unlabeled examples, 0 labeled.

#### **Scoring function advice:**

- Penalties only, so 0 = best.
- Can use varying magnitudes, -1, -5, -10.
- Debug with some stochastic optimization.

### Citation Field Extraction Accuracy

Method (no labeled data)	Token accuracy	Time sec/citation	Ave. V() score	
GE [Mann & McCallum '10]	37%	?	N/A	
V search 10	34%	14	-1.86	
V search 100	39%	170	-0.98	
V search 1000	42%	1240	-0.62	
SPEN	52%	0.0008	~ -20	



#### Example text

Wright, A. K. Simple imperative polymorphism. Lisp and Symbolic Computation 8, 4 (Dec. 1995), 343-356.

#### V search 100 output



АЛТНО	AUTHO	АЛТНС	AUTHC	АОТНС	NO	NO	ON	NO	ON ON	DA	DA	<b> </b>
SPE	N ou	<u>tput</u>										
UTHOR		TITLE	116	THE	TITLE	TILLE	116	THE	TITLE	DATE	DATE	PAGES PAGES PAGES
4												

#### **Related Work**

Deep Value Networks...

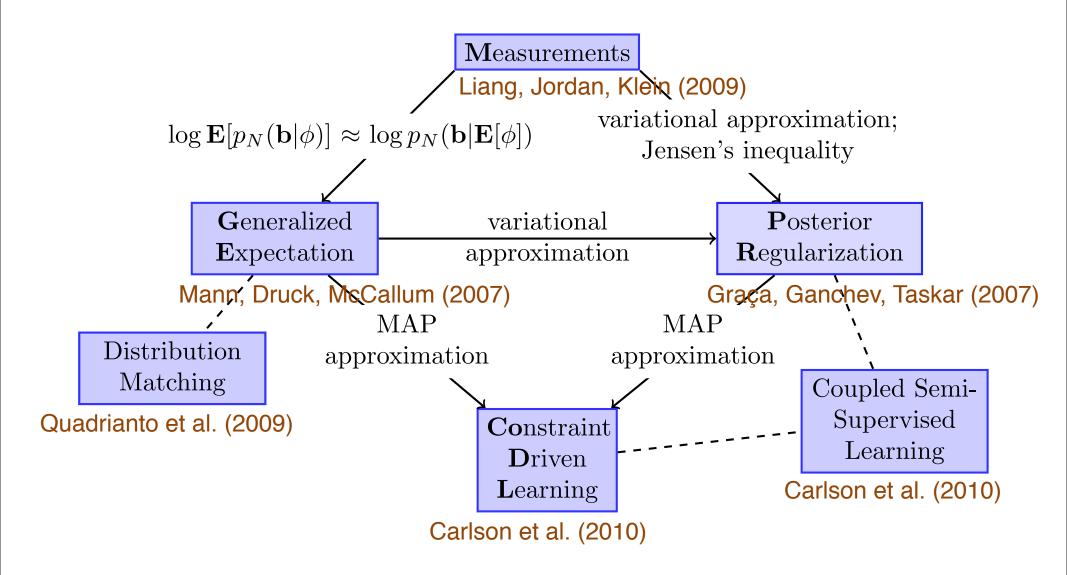
[Gygli, Norouzi, Angelova 2017 ICML]

- Matching magnitude (rather than just ranking).
- Hurts accuracy? 5% vs SPEN's 52%
- Constraint-Driven Learning

[Chang, Ratinov, Roth 2007 ACL]

- Supervised training → Pseudo-label data w/ constraints →
- Snorkel: Rapid Training Data Creation with Weak Supervision [Ratner, Bach, Ehrenberg, Fries, Wu, Ré 2017 VLDB]
  - Rules → Pseudo-labeled data → Supervised (self) training
- Label-Free Supervision of NNs w/ ... Domain Knowledge [Stewart, Ermon 2017 AAAI]
  - Constraints → Loss function → Train feed-forward NN.

#### **GE Related Work**



### Summary

#### Generalized Expectation

- Learning from unlabeled data + "labeled features"
- Hard to do inference

#### Structured Prediction Energy Networks

- Representation learning for output variables
- Test-time inference by gradient descent
- New SPEN training method: Ranking

#### Experiments

- Multi-label Classification: ICM-9
- Sequence labeling: Citation field extraction

#### Next

- Training on corpus-wide expectations.
- Interactive tools for score function development.