# Learning from Limited Labeled Data (but a lot of unlabeled data)

NELL as a case study

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### Thesis:

We will never really understand learning until we build machines that

- learn many different things,
- from years of diverse experience,
- in a staged, curricular fashion,
- and become better <u>learners</u> over time.

## **NELL: Never-Ending Language Learner**

#### The task:

- run 24x7, forever
- each day:
  - 1. extract more facts from the web to populate the ontology
  - learn to read (perform #1) better than yesterday

### Inputs:

- initial ontology (categories and relations)
- dozen examples of each ontology predicate
- the web
- occasional interaction with human trainers

## **NELL** today

Running 24x7, since January, 12, 2010

### Result:

- KB with ~120 million confidence-weighted beliefs
- learning to read
- learning to reason
- extending ontology

#### NELL knowledge fragment football uses \* including only correct beliefs equipment climbing helmet skates Canada Sunnybrook Miller uses equipment citv country hospital Wilson company hockey **Detroit** GM politician **CFRB** radio Pearson **Toronto** hometown play hired competes airport home town with **Stanley** citv **Maple Leafs** Red company city Wings Toyota stadium team stadium league league Connaught city acquired paper city Air Canada NHL member created stadium Hino Centre plays in economic sector **Globe and Mail** Sundin **Prius** writer automobile Toskala **Skydome** Corrola Milson

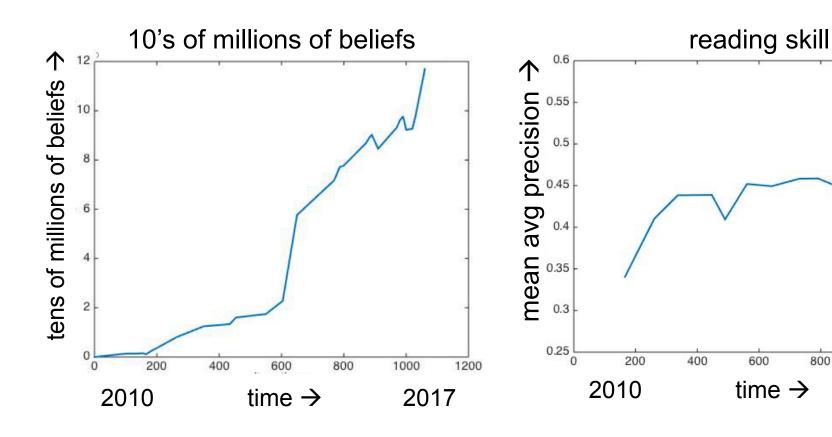
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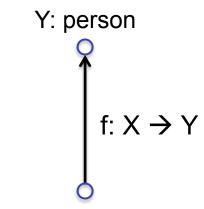
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## **Improving Over Time** Never Ending Language Learner



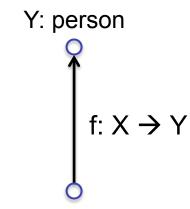


X: noun phrase

### hard

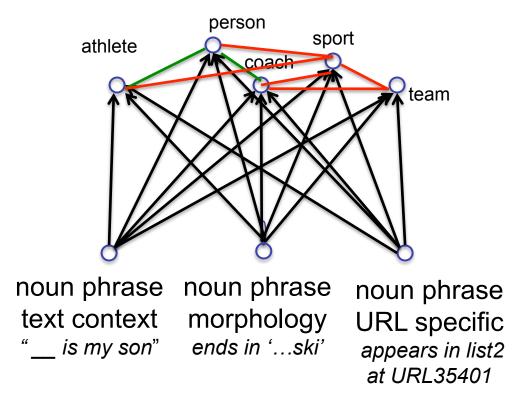
(underconstrained) semi-supervised learning

### Key Idea: Massively coupled semi-supervised training



X: noun phrase

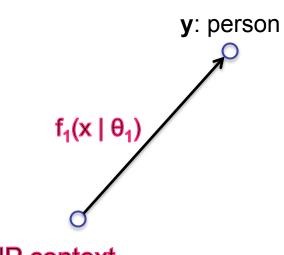
hard (underconstrained) semi-supervised learning



### much easier

(more constrained) semi-supervised learning

### **Supervised training of 1 function:**



$$\theta_1 = \arg\min_{\theta_1}$$

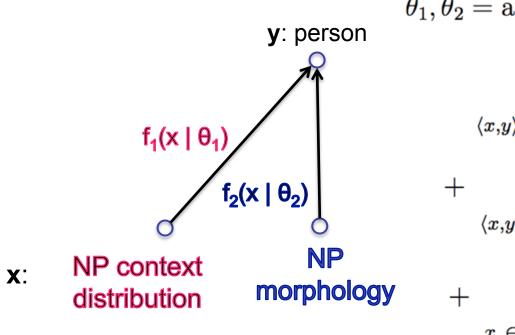
$$\sum_{\langle x,y\rangle \in labeled \ data} |f_1(x|\theta_1) - y|$$

x: NP context distribution

\_\_ is a friend rang the \_\_

\_\_ walked in

### Coupled training of 2 functions:



$$heta_1, heta_2 = rg\min_{ heta_1, heta_2}$$

$$\sum_{\langle x,y\rangle \in labeled \ data} |f_1(x|\theta_1) - y|$$

$$+ \sum_{\langle x,y\rangle \in labeled \ data} |f_2(x|\theta_2) - y|$$

+ 
$$\sum_{x \in unlabeled \ data} |f_1(x|\theta_1) - f_2(x|\theta_2)|$$

\_\_ is a friend capitalized?
rang the \_\_ ends with '...ski'?
...
walked in contains "univ."?

### NELL Learned Contexts for "Hotel" (~1% of total)

"\_ is the only five-star hotel" "\_ is the only hotel" "\_ is the perfect accommodation" "\_ is the perfect address" "\_ is the perfect lodging" "\_ is the sister hotel" " is the ultimate hotel" " is the value choice" " is uniquely situated in" "\_ is Walking Distance" "\_ is wonderfully situated in" "\_ las vegas hotel" "\_ los angeles hotels" "\_ Make an online hotel reservation" "\_ makes a great home-base" "\_ mentions Downtown" "\_ mette a disposizione" "\_ miami south beach" "\_ minded traveler" "\_ mucha prague Map Hotel" " n'est qu'quelques minutes" "\_ naturally has a pool" "\_ is the perfect central location" "\_ is the perfect extended stay hotel" "\_ is the perfect headquarters" "\_ is the perfect home base" " is the perfect lodging choice" " north reddington beach" "\_ now offer guests" "\_ now offers guests" "\_ occupies a privileged location" "\_ occupies an ideal location" "\_ offer a king bed" "\_ offer a large bedroom" " offer a master bedroom" "\_ offer a refrigerator" "\_ offer a separate living area" "\_ offer a separate living room" "\_ offer comfortable rooms" "\_ offer complimentary shuttle service" "\_ offer deluxe accommodations" "\_ offer family rooms" " offer secure online reservations" " offer upscale amenities" "\_ offering a complimentary continental breakfast" "\_ offering comfortable rooms" "\_ offering convenient access" "\_ offering great lodging" "\_ offering luxury accommodation" "\_ offering world class facilities" "\_ offers a business center" "\_ offers a business centre" "\_ offers a casual elegance" "\_ offers a central location" " surrounds travelers" ...

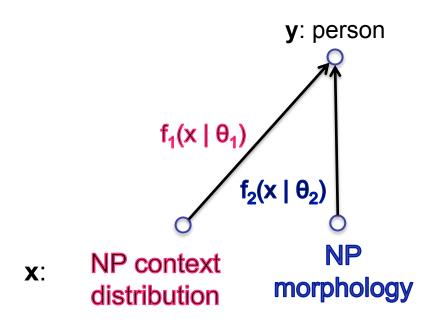
## NELL Highest Weighted\* string fragments: "Hotel"

```
1.82307 SUFFIX=tel
```

- 1.81727 SUFFIX=otel
- 1.43756 LAST\_WORD=inn
- 1.12796 PREFIX=in
- 1.12714 PREFIX=hote
- 1.08925 PREFIX=hot
- 1.06683 SUFFIX=odge
- 1.04524 SUFFIX=uites
- 1.04476 FIRST\_WORD=hilton
- 1.04229 PREFIX=resor
- 1.02291 SUFFIX=ort
- 1.00765 FIRST WORD=the
- 0.97019 SUFFIX=ites
- 0.95585 FIRST WORD=le
- 0.95574 PREFIX=marr
- 0.95354 PREFIX=marri
- 0.93224 PREFIX=hyat
- 0.92353 SUFFIX=yatt
- 0.88297 SUFFIX=riott
- 0.88023 PREFIX=west
- 0.87944 SUFFIX=iott

<sup>\*</sup> logistic regression

## Type 1 Coupling: Co-Training, Multi-View Learning



#### Theorem (Blum & Mitchell, 1998):

If f<sub>1</sub>,and f<sub>2</sub> are PAC learnable from noisy labeled data, and X<sub>1</sub>, X<sub>2</sub> are conditionally independent given Y,

Then f<sub>1</sub>, f<sub>2</sub> are PAC learnable from polynomial *unlabeled* data plus a weak initial predictor

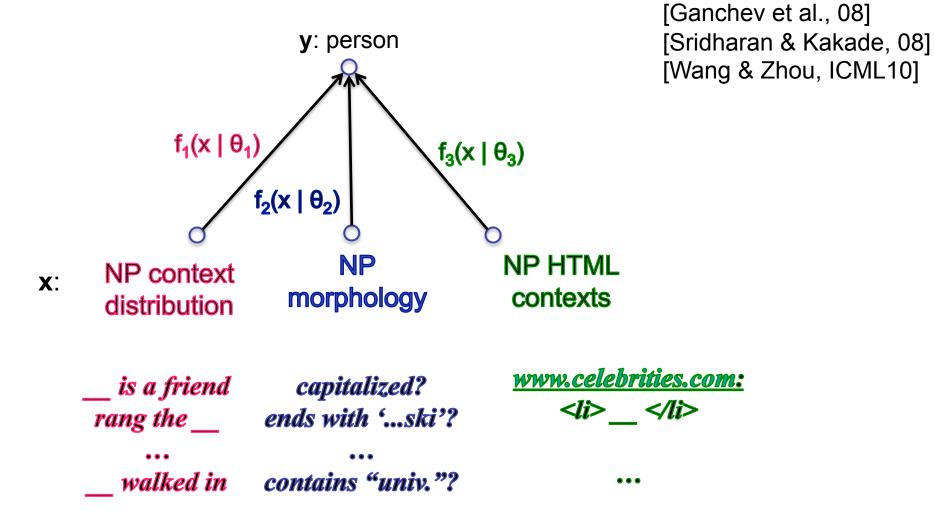
```
__ is a friend capitalized?
rang the __ ends with '...ski'?
... ...
walked in contains "univ."?
```

## Type 1 Coupling: Co-Training, Multi-View Learning

[Blum & Mitchell; 98]

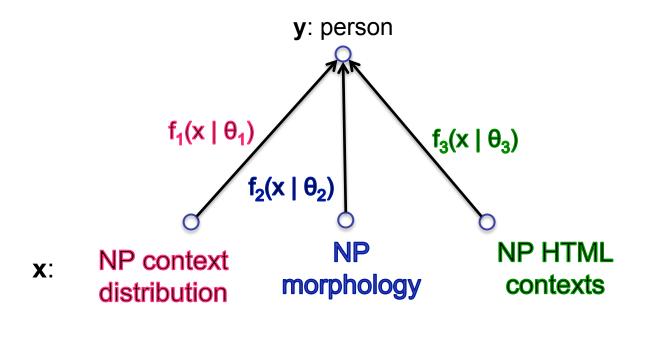
[Dasgupta et al; 01]

[Balcan & Blum; 08]



## Type 1 Coupling: Co-Training, Multi-View Learning

sample complexity drops exponentially in the number of views of X



[Blum & Mitchell; 98] [Dasgupta et al; 01] [Balcan & Blum; 08] [Ganchev et al., 08] [Sridharan & Kakade, 08] [Wang & Zhou, ICML10]

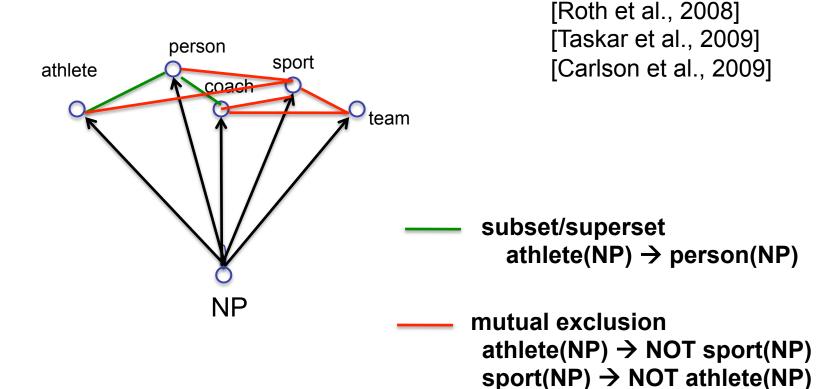
www.celebrities.com: is a friend capitalized? rang the ends with '...ski'?

walked in

contains "univ."?

\_\_

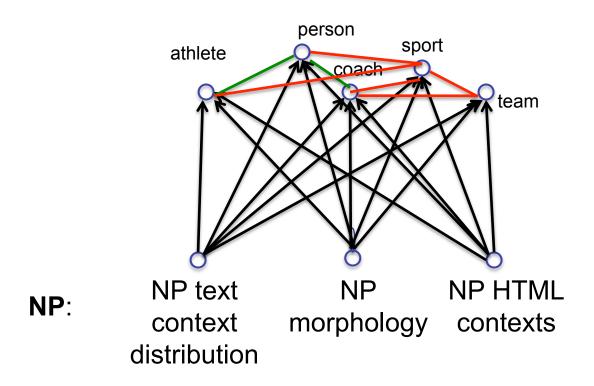
## Type 2 Coupling: Multi-task, Structured Outputs

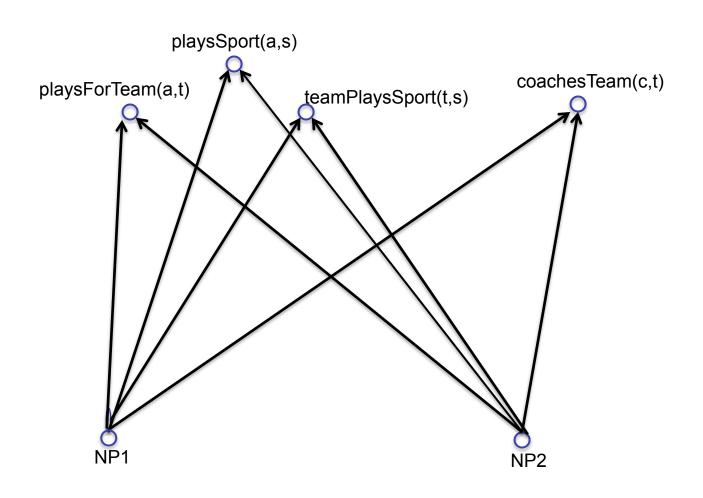


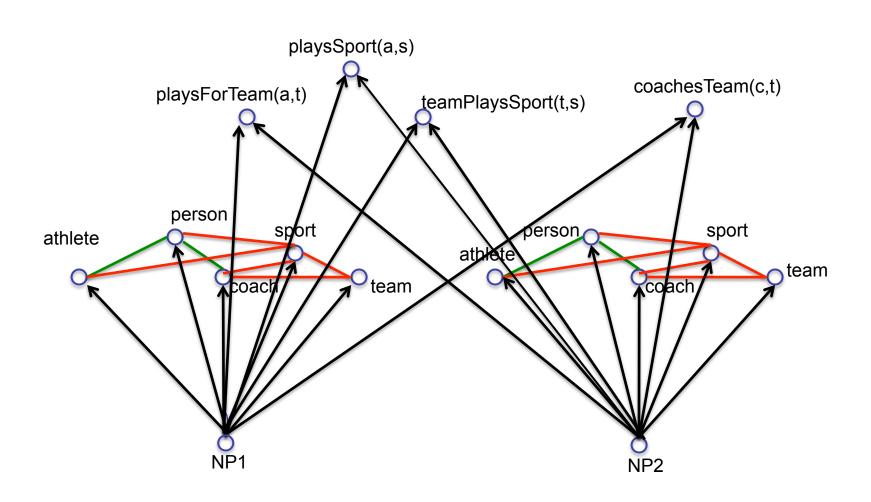
[Daume, 2008]

[Bakhir et al., eds. 2007]

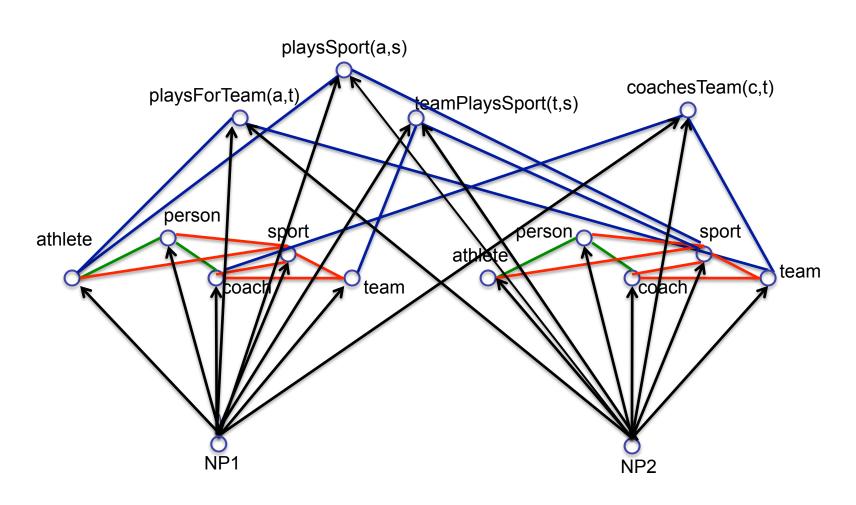
## Multi-view, Multi-Task Coupling



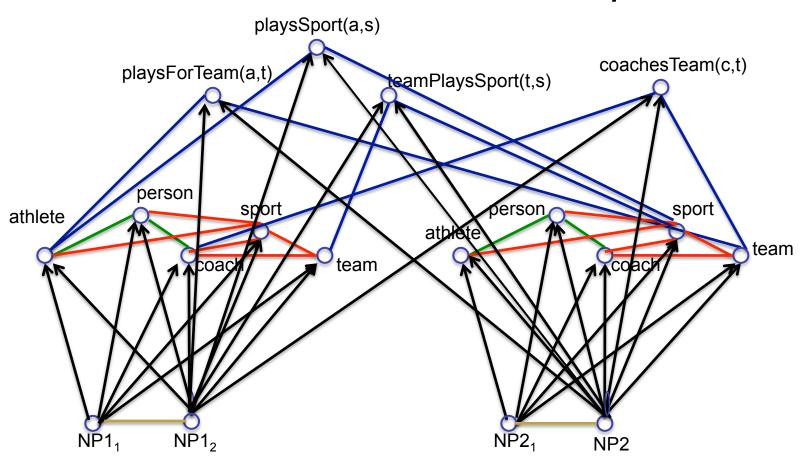




playsSport(NP1,NP2) → athlete(NP1), sport(NP2)



### over 4000 coupled functions in NELL



multi-view consistencyargument type consistency

subset/superset mutual exclusion

### How to train

### approximation to EM:

- E step: predict beliefs from unlabeled data (ie., the KB)
- M step: retrain

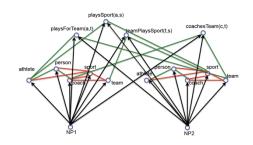
### **NELL** approximation:

- bound number of new beliefs per iteration, per predicate
- rely on multiple iterations for information to propagate, partly through joint assignment, partly through training examples

### Better approximation:

 Joint assignments based on probabilistic soft logic [Pujara, et al., 2013] [Platanios et al., 2017] If coupled learning is the key, how can we get new coupling constraints?

## Key Idea 2:



## Learn new coupling constraints

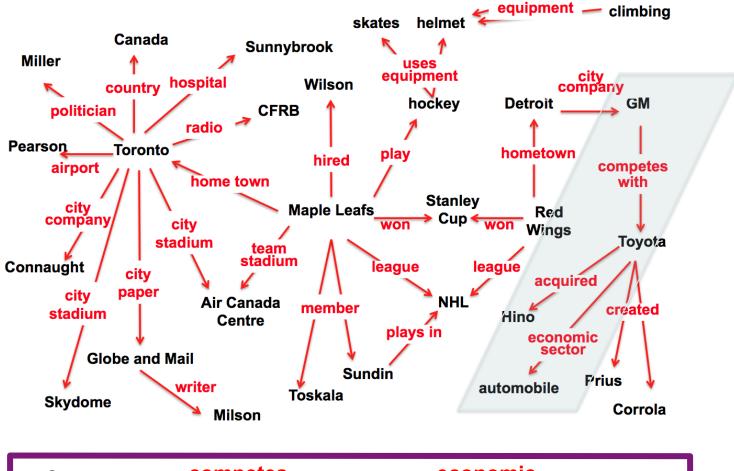
first order, probabilistic horn clause constraints:

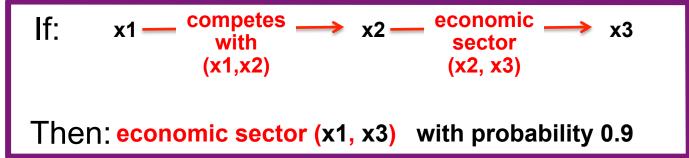
0.93 athletePlaysSport(?x,?y) ← athletePlaysForTeam(?x,?z) teamPlaysSport(?z,?y)

- learned by data mining the knowledge base
- connect previously uncoupled relation predicates
- infer new unread beliefs
- NELL has 100,000s of learned rules
- uses PRA random-walk inference [Lao, Cohen, Gardner]

### Key Idea 2: Learn inference rules

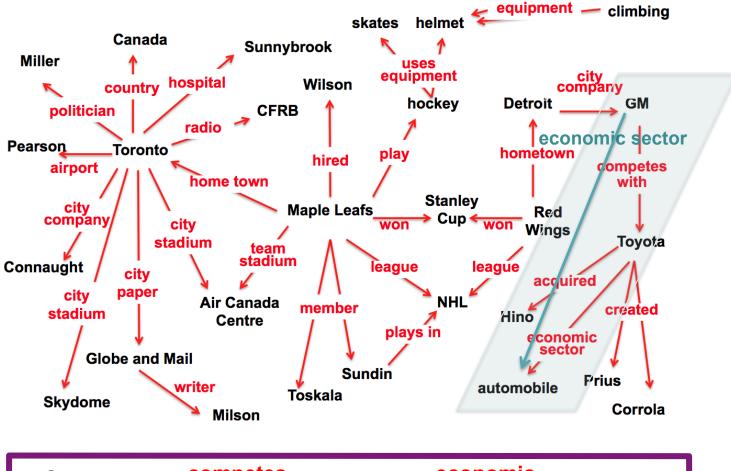
PRA: [Lao, Mitchell, Cohen, EMNLP 2011]

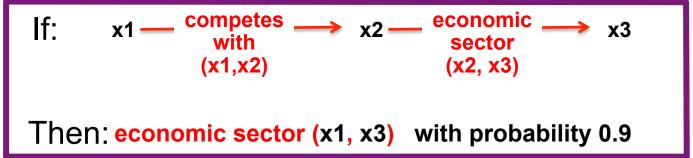




### Key Idea 2: Learn inference rules

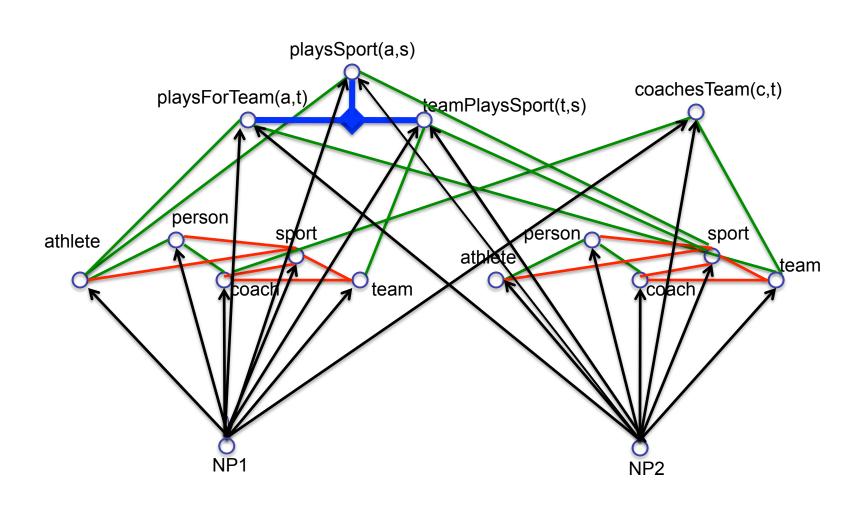
PRA: [Lao, Mitchell, Cohen, EMNLP 2011]





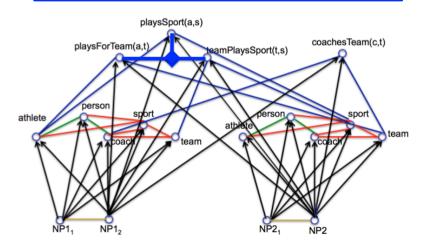
## Learned Rules are New Coupling Constraints!

0.93 playsSport(?x,?y)  $\leftarrow$  playsForTeam(?x,?z), teamPlaysSport(?z,?y)



## Learned Rules are New Coupling Constraints!

0.93 playsSport(?x,?y) ← playsForTeam(?x,?z), teamPlaysSport(?z,?y)



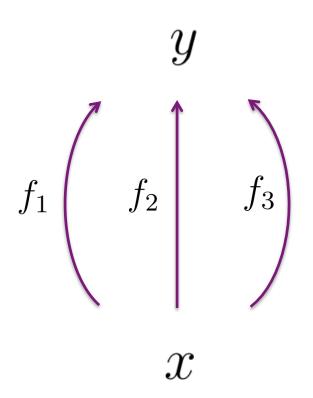
- Learning X makes one a better <u>learner</u> of Y
- Learning Y makes one a better <u>learner</u> of X
  - $X = reading functions: text \rightarrow beliefs$
  - Y = Horn clause rules: beliefs → beliefs

## **Consistency and Correctness**

what is the relationship?
under what conditions?
link between learning and error estimation

### Problem setting:

• have N different estimates  $f_1, \dots f_N$  of target function  $f^*$   $y = f^*(x); y \in \{0, 1\}$ 



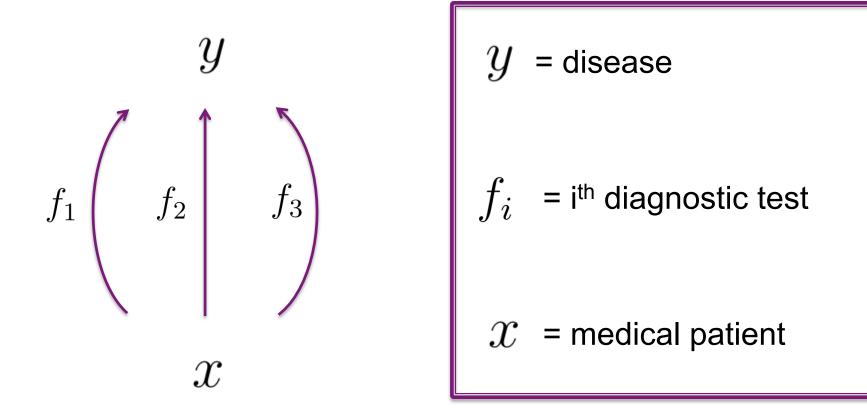
$$y$$
 = NELL category "city"

$$f_i$$
 = classifier based on i<sup>th</sup> view of  $x$ 

 $\mathcal{X}$  = noun phrase

### Problem setting:

• have N different estimates  $f_1, \ldots f_N$  of target function  $f^*$ 



[Hui & Walter, 1980; Collins & Huynh, 2014]

[Platanios, Blum, Mitchell]

### Problem setting:

• have N different estimates  $f_1, \dots f_N$  of target function  $f^*$  $f^*: X \to Y; Y \in \{0, 1\}$ 

### Goal:

• estimate accuracy of each of  $f_1, \ldots f_N$  from **unlabeled** data

### Problem setting:

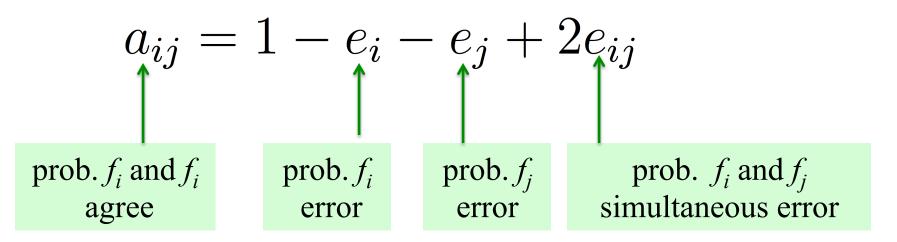
- have N different estimates  $f_1, \dots f_N$  of target function  $f^*$  $f^*: X \to Y; \ Y \in \{0, 1\}$
- agreement between  $f_i, f_j: a_{ij} \equiv P_x(f_i(x) = f_j(x))$

### Problem setting:

- have N different estimates  $f_1, \dots f_N$  of target function  $f^*$  $f^*: X \to Y; Y \in \{0, 1\}$
- agreement between  $f_i, f_j: a_{ij} \equiv P_x(f_i(x) = f_j(x))$

Key insight: errors and agreement rates are related agreement can be estimated from unlabeled data

 $a_{ij} = \Pr[\text{neither makes error}] + \Pr[\text{both make error}]$ 



## **Estimating Error from Unlabeled Data**

1. IF  $f_1$ ,  $f_2$ ,  $f_3$  make independent errors, and accuracies > 0.5

then 
$$a_{ij} = 1 - e_i - e_j + 2e_{ij}$$
 becomes 
$$a_{ij} = 1 - e_i - e_j + 2e_ie_j$$

Determine errors from unlabeled data!

- use unlabeled data to estimate  $a_{12}$ ,  $a_{13}$ ,  $a_{23}$
- solve three equations for three unknowns  $e_1$ ,  $e_2$ ,  $e_3$

## Estimating Error from Unlabeled Data

1. IF  $f_1$ ,  $f_2$ ,  $f_3$  make indep. errors, accuracies > 0.5 then  $a_{ij}=1-e_i-e_j+2e_{ij}$  becomes  $a_{ij}=1-e_i-e_j+2e_ie_j$ 

2. but if errors **not** independent

## **Estimating Error from Unlabeled Data**

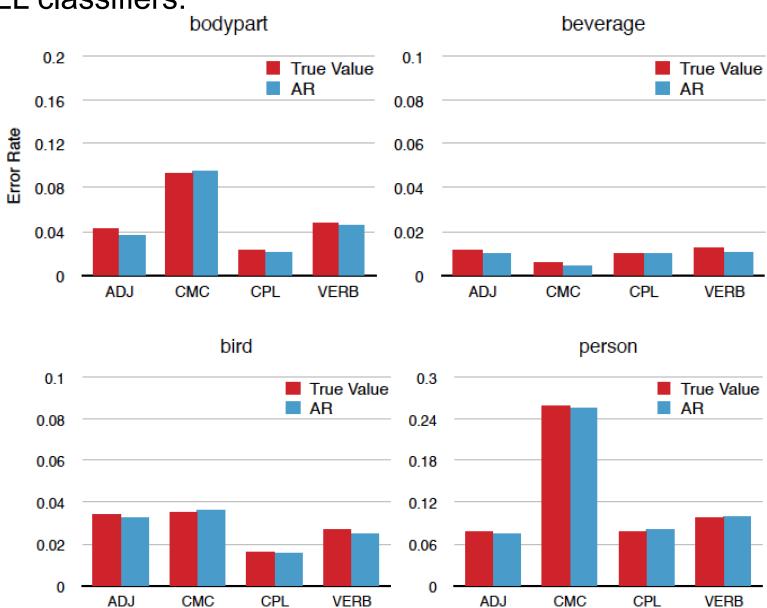
- 1. IF  $f_i$ ,  $f_2$ ,  $f_3$  make indep. errors, accuracies > 0.5 then  $a_{ij}=1-e_i-e_j+2e_{ij}$  becomes  $a_{ij}=1-e_i-e_j+2e_ie_j$
- 2. but if errors **not** independent, add prior: the more independent, the more probable

min 
$$\sum_{i,j} (e_{ij} - e_i e_j)^2$$
  
such that 
$$(\forall i,j) \ a_{ij} = 1 - e_i - e_j + 2e_{ij}$$

## True error (red), estimated error (blue)

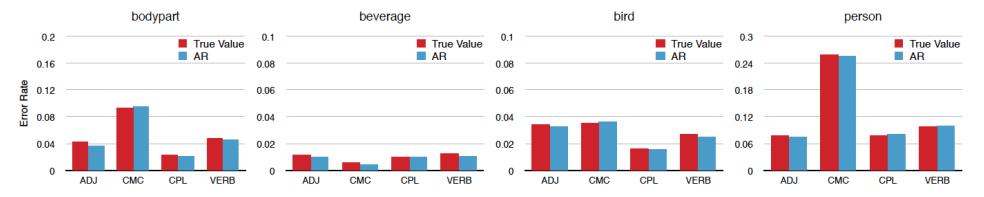
**NELL** classifiers:

[Platanios et al., 2014]

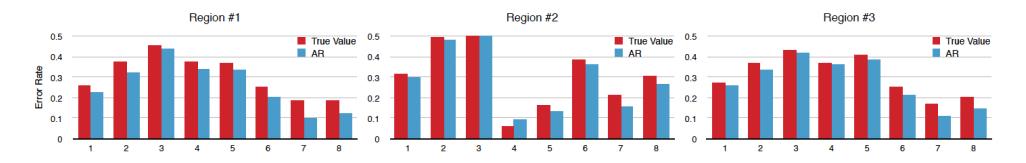


## True error (red), estimated error (blue) [Platanios, Blum, Mitchell]

### **NELL** classifiers:



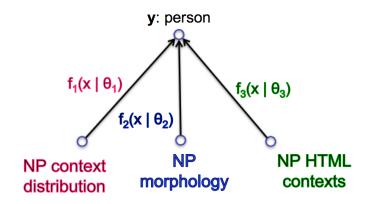
### Brain image fMRI classifiers:



## Multiview setting

Given functions  $f_i: X_i \rightarrow \{0,1\}$  that

- make independent errors
- are better than chance



### If you have at least 2 such functions

 they can be <u>PAC learned</u> by training them to agree over unlabeled data [Blum & Mitchell, 1998]

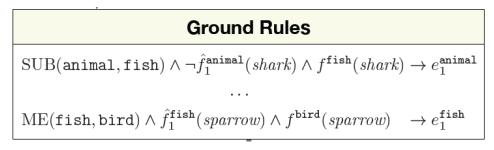
### If you have at least 3 such functions

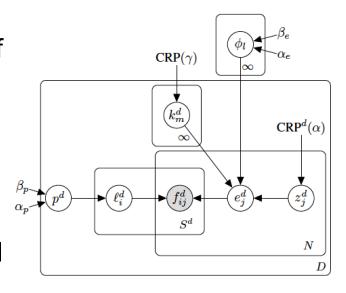
 their <u>accuracy</u> can be calculated from agreement rates over unlabeled data [Platanios et al., 2014]

Is accuracy estimation strictly harder than learning?

## More on Accuracy Estimation

- Graphical model approach, learns clusters of target functions, and clusters of classifier types to share parameters: "Estimating Accuracy from Unlabeled Data: A Bayesian Approach", ICML, Platanios et. al., 2016
- Logical approach using PSL to model mutual exclusion and subsumption constraints.
   Outputs both error rates and estimated labels. "Estimating Accuracy from Unlabeled Data: A Logical Approach," NIPS, Platanios et. al, 2017





### Conclusions

- To make semi-supervised learning easier, couple training of many functions
  - and learn new consistency coupling constraints over time
- Consistency vs. Correctness
  - coupled training + initial assumptions ->

     increasing consistency = increasing correctness ]
- Accuracy can be estimated from rate of consistency
- Open questions:
  - under what conditions does consistency → correctness?
  - what architectures for learning agents can achieve these conditions?
  - is unlabeled accuracy estimation harder than unlabeled learning?

## thank you!



follow NELL on Twitter: @CMUNELL browse/download NELL's KB at <a href="http://rtw.ml.cmu.edu">http://rtw.ml.cmu.edu</a>