Meta-Learning for Semi-Supervised Few-Shot Classification

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Abstract

In this work, we advance the few-shot classification paradigm towards a scenario where unlabeled examples are also available within each episode. We consider two situations: one where all unlabeled examples are assumed to belong to the same set of labeled classes of the episode, as well as the more challenging situation where examples from other distractor classes are also provided. To address this paradigm, we propose novel extensions of Prototypical Networks that are augmented with the ability to use unlabeled examples when producing prototypes. These models are trained in an end-to-end way on episodes, to learn to leverage the unlabeled examples successfully. We also propose a new split of ImageNet, consisting of a large set of classes, with a hierarchical structure. Our experiments confirm that our Prototypical Networks can learn to improve their predictions due to unlabeled examples, much like a semi-supervised algorithm would.

1 Introduction

The availability of large quantities of labeled data has enabled deep learning methods to achieve impressive breakthroughs in several tasks related to artificial intelligence, such as speech recognition, object recognition and machine translation. However, current deep learning approaches struggle in tackling problems for which labeled data are scarce.

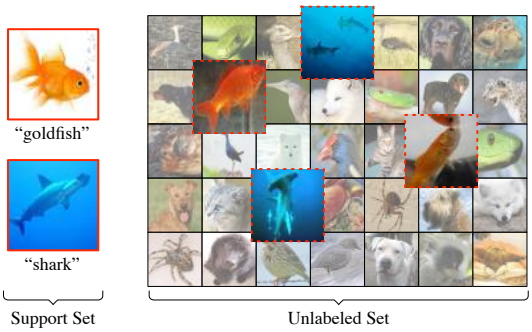

Figure 1: Consider a setup where the aim is to learn a classifier to distinguish between two previously unseen classes, goldfish and shark, given not only labeled examples of these two classes, but also a larger pool of unlabeled examples, some of which may belong to one of these two classes of interest.

For this reason, recently there has been an increasing body of work on few-shot learning, which considers the design of learning algorithms that specifically allow for better generalization on problems with small labeled training sets. Here we focus on the case of few-shot classification, where the given classification problem is assumed to contain only a handful of labeled examples per class. One approach to few-shot learning follows a form of meta-learning[2] [1, 2], which performs transfer learning from a pool of various classification problems generated from large quantities of available labeled data, to new classification problems from classes unseen at training time. Meta-learning may take the form

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[2]See the following blog post for an overview: `http://bair.berkeley.edu/blog/2017/07/18/learning-to-learn/`

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of learning a shared metric [3, 4], a common initialization for few-shot classifiers [5, 6] or a generic inference network [7, 8].

However, this progress has been in a limited scenario, which differs in many dimensions from how humans learn new concepts. In this paper we aim to generalize the few-shot setting in two ways. First we consider a scenario in which the new classes are learned in the presence of additional unlabeled data. Second, we consider the situation where the new classes to be learned are not viewed in isolation. Instead, many of the unlabeled examples are from different classes; the presence of such *distractor* classes introduces an additional and more realistic level of difficulty to the few-shot problem. We propose and study three novel extensions of Prototypical Networks [4], a state-of-the-art approach to few-shot learning, to the semi-supervised setting. We demonstrate in our experiments that our semi-supervised variants successfully learn to leverage unlabeled examples and outperform purely supervised Prototypical Networks.

2 Semi-Supervised Few-Shot Learning

We denote our training set as a tuple of labeled and unlabeled examples: $(\mathcal{S}, \mathcal{R})$. The labeled portion is the usual support set $\mathcal{S}$ of the few-shot learning literature, containing a list of tuples of inputs and targets. In addition to classic few-shot learning, we introduce an unlabeled set $\mathcal{R}$ containing only inputs: $\mathcal{R} = \{\tilde{\boldsymbol{x}}_1, \tilde{\boldsymbol{x}}_2, \ldots, \tilde{\boldsymbol{x}}_M\}$. As in the purely supervised setting, our models are trained to perform well when predicting the labels for the examples in the episode's query set $\mathcal{Q}$. Figure 2 shows a visualization of training and test episodes.

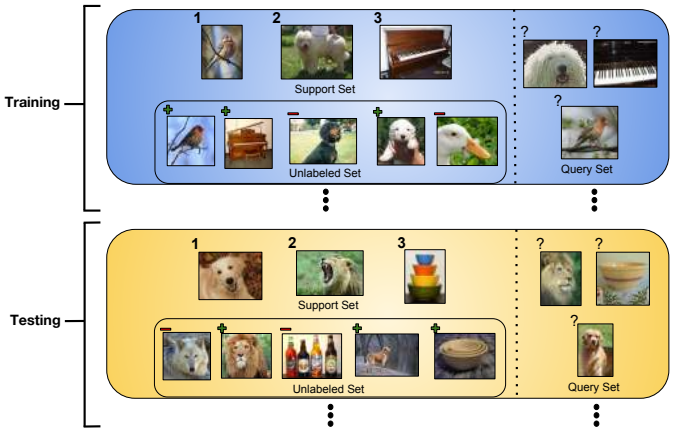

Figure 2: Example of the semi-supervised few-shot learning setup. Training episodes consist of a support set $\mathcal{S}$, an unlabeled set $\mathcal{R}$, and a query set $\mathcal{Q}$. The items in $\mathcal{R}$ may either be pertinent to the labeled classes (with + signs) or they may be *distractor* items (with - signs).

2.1 Prototypical Networks with Soft k-Means

We first consider a simple way of leveraging unlabeled examples for refining prototypes, by taking inspiration from semi-supervised clustering. One natural choice would be to borrow from the inference performed by soft k-means. We prefer this version of k-means over hard assignments since hard assignments would make the inference non-differentiable. We start from the regular Prototypical Network [4]'s prototypes $\boldsymbol{p}_c$. Then, the unlabeled examples get a partial assignment $(\tilde{z}_{j,c})$ to each cluster based on their Euclidean distance to the cluster locations. Finally, refined prototypes are obtained by incorporating these unlabeled examples.

This process can be summarized as follows:

$$\tilde{\boldsymbol{p}}_c = \frac{\sum_i h(\boldsymbol{x}_i) z_{i,c} + \sum_j h(\tilde{\boldsymbol{x}}_j) \tilde{z}_{j,c}}{\sum_i z_{i,c} + \sum_j \tilde{z}_{j,c}}, \quad \text{where} \quad \tilde{z}_{j,c} = \frac{\exp\left(-||h(\tilde{\boldsymbol{x}}_j) - \boldsymbol{p}_c||_2^2\right)}{\sum_{c'} \exp\left(-||h(\tilde{\boldsymbol{x}}_j) - \boldsymbol{p}_{c'}||_2^2\right)} \tag{1}$$

We could perform several iterations of refinement, as is usual in k-means. However, we have experimented with various number of iterations and found results to not improve beyond a single refinement step.

2.2 Prototypical Networks with Soft k-Means with a Distractor Cluster

The soft k-means approach described above implicitly assumes that each unlabeled example belongs to either one of the N classes in the episode. However, it would be much more general to have a model robust to the existence of examples from other classes, which we refer to as distractor

classes. A simple way to address this is to add an additional cluster whose purpose is to capture the distractors.

$$\boldsymbol{p}_c = \begin{cases} \frac{\sum_i h(\boldsymbol{x}_i) z_{i,c}}{\sum_i z_{i,c}} & \text{for } c = 1...N \\ \mathbf{0} & \text{for } c = N+1 \end{cases} \tag{2}$$

Here we take the simplifying assumption that the distractor cluster has a prototype centered at the origin. We also consider introducing length-scales r_c to represent variations in the within-cluster distances, specifically for the distractor cluster:

$$\tilde{z}_{j,c} = \frac{\exp\left(-\frac{1}{r_c^2}||\tilde{\boldsymbol{x}}_j - \boldsymbol{p}_c||_2^2 - A(r_c)\right)}{\sum_{c'} \exp\left(-\frac{1}{r_c^2}||\tilde{\boldsymbol{x}}_j - \boldsymbol{p}_{c'}||_2^2 - A(r_{c'})\right)}, \text{ where } A(r) = \frac{1}{2}\log(2\pi) + \log(r) \tag{3}$$

For simplicity, we set $r_{1...N}$ to 1 in our experiments, and only learn the length-scale of the distractor cluster r_{N+1}.

2.3 Prototypical Networks with Soft k-Means and Masking

Modeling distractor unlabeled examples with a single cluster is likely too simplistic , since distractor examples may very well cover more than a single natural object category. To address this problem, we incorporate a soft-masking mechanism on the contribution of unlabeled examples. We start by computing normalized distances $\tilde{d}_{j,c}$ between examples $\tilde{\boldsymbol{x}}_j$ and prototypes $\boldsymbol{p}_c$:

$$\tilde{d}_{j,c} = \frac{d_{j,c}}{\frac{1}{M}\sum_j d_{j,c}}, \text{ where } d_{j,c} = ||h(\tilde{\boldsymbol{x}}_j) - \boldsymbol{p}_c||_2^2 \tag{4}$$

Then, soft thresholds β_c and slopes γ_c are predicted for each prototype, by feeding to a small neural network various statistics of the normalized distances for the prototype:

$$[\beta_c, \gamma_c] = \text{MLP}\left([\min_j(\tilde{d}_{j,c}), \max_j(\tilde{d}_{j,c}), \text{var}_j(\tilde{d}_{j,c}), \text{skew}_j(\tilde{d}_{j,c}), \text{kurt}_j(\tilde{d}_{j,c})]\right) \tag{5}$$

This allows each threshold to use information on the amount of intra-cluster variation to determine how aggressively it should cut out unlabeled examples.

Then, soft masks $m_{j,c}$ for the contribution of each example to each prototype are computed, by comparing to the threshold the normalized distances, as follows:

$$\tilde{\boldsymbol{p}}_c = \frac{\sum_i h(\boldsymbol{x}_i) z_{i,c} + \sum_j h(\tilde{\boldsymbol{x}}_j)\tilde{z}_{j,c} m_{j,c}}{\sum_i z_{i,c} + \sum_j \tilde{z}_{j,c} m_{j,c}}, \text{ where } m_{j,c} = \sigma\left(-\gamma_c\left(\tilde{d}_{j,c} - \beta_c\right)\right) \tag{6}$$

where $\sigma(\cdot)$ is the sigmoid function.

3 Experiments

3.1 Datasets

We evaluate the performance of our models on three datasets: two benchmark few-shot classification datasets and a novel large-scale dataset that we hope will be useful for future few-shot learning work.

Omniglot [9] is a dataset of 1,623 handwritten characters from 50 alphabets. Each character was drawn by 20 human subjects. We follow the few-shot setting proposed by [3], in which the images are resized to 28×28 pixels and rotations in multiples of 90° are applied, yielding 6,492 classes in total. These are split into 4,800 training classes and 1,692 classes for test. 10% of the training images are used as labeled examples.

***mini*ImageNet** [3] is a modified version of the ILSVRC-12 dataset [10], in which 600 images for each of 100 classes were randomly chosen to be part of the dataset. We rely on the class split used by [5]. These splits use 64 classes as training, 16 for validation, and 20 for test. All images are of size 84×84 pixels. 40% of the training images are used as labeled examples.

***tiered*ImageNet** is our proposed dataset for few-shot classification. Like *mini*Imagenet, it is a subset of ILSVRC-12. However, *tiered*ImageNet represents a larger subset of ILSVRC-12 (608

ProtoNet Model	Err.	Err. w/ D
Supervised	5.16%	5.16%
Semi-Supervised Inference	2.35%	4.70%
Soft k-Means	2.56%	4.59%
Soft k-Means+Cluster	**2.18%**	2.71%
Masked Soft k-Means	2.46%	**2.62%**

Table 1: Omniglot 1-shot Results

ProtoNet Model	*mini* / *tiered* 1-shot Acc.	*mini* / *tiered* 5-shot Acc.	*mini* / *tiered* 1-shot Acc. w/ D	*mini* / *tiered* 5-shot Acc. w/ D
Supervised	43.36% / 46.60%	59.03% / 67.18%	43.36% / 46.60%	59.03% / 67.18%
Semi-Supervised Inference	48.68% / 50.38%	62.94% / 70.26%	46.16% / 46.87%	62.32% / 68.38%
Soft k-Means	48.25% / 53.41%	**65.72% / 71.31%**	46.72% / 50.18%	61.94% / 68.83%
Soft k-Means+Cluster	**50.87% / 55.82%**	63.75% / 70.79%	48.60% / 49.87%	61.51% / 70.16%
Masked Soft k-Means	50.57% / 52.76%	63.78% / 70.08%	**50.04% / 50.93%**	**62.50% / 71.00%**

Table 2: *mini*ImageNet and *tiered*ImageNet 1/5-shot Results

classes rather than 100 for *mini*ImageNet). Analogous to Omniglot, in which characters are grouped into alphabets, *tiered*ImageNet groups classes into broader categories corresponding to higher-level nodes in the ImageNet [11] hierarchy. There are 34 categories in total, with each category containing between 10 and 30 classes. These are split into 20 training categories, 6 validation categories, and 8 testing categories. (details of the dataset can be found in the Supplementary Materials). This ensures that all of the training classes are sufficiently distinct from the testing classes, unlike *mini*ImageNet and other alternatives such as *rand*ImageNet proposed by [3]. For example, "pipe organ" is a training class and "electric guitar" is a test class in the [5] split of *mini*Imagenet, even though they are both musical instruments. 10% of the training images are used as labeled examples.

In each dataset we compare our three semi-supervised models with two baselines. The first baseline, referred to as Supervised in our tables, is an ordinary Prototypical Network that is trained in a purely supervised way on the labeled split of each dataset. The second baseline, referred to as Semi-Supervised Inference, uses the embedding function learned by this supervised Prototypical Network, but performs semi-supervised refinement of the prototypes at inference time using a step of Soft k-Means refinement. For *tiered*ImageNet, We report the final test accuracy trained with both training and validation set.

3.2 Results

Results for Omniglot are given in Table 1, and *mini*ImageNet and *tiered*ImageNet in Table 2. Across all three benchmarks, at least one of our proposed models outperform the baselines, demonstrating the effectiveness of our semi-supervised meta-learning procedure. In particular, Soft k-means+Cluster performs the best on 1-shot non-distractor settings, as the extra cluster seems to provide a form of regularization that pushes the clusters farther apart. Soft k-Means performs well on 5-shot non-distractor settings, as it considers the most unlabeled examples. Masked Soft k-Means shows the most robust performance in distractors settings, in both 1-shot and 5-shot tasks. For 5-shot, Masked soft k-Means reaches comparable performance compared to the upper bound of the best non-distractor performance.

From Figure 3, we observe clear improvement in test accuracy when the number grows from 0 to 25. Note that our models were trained with $M = 5$ and thus are showing an ability to extrapolate in generalization. This confirms that, through meta-training, the models learned to acquire a better representation that will be more helpful after semi-supervised refinement.

Note that the wins obtained in our semi-supervised learning are super-additive. Consider the case of the simple k-Means model on 1-shot without Distractors. Training only on labeled examples while incorporating the unlabeled set during test time produces an advantage of 3.8% (50.4-46.6), while incorporating the unlabeled set during training but not during test produces a win of 1.1% (47.7-46.6). Incorporating unlabeled examples during both training and test yields a win of 6.8% (53.4-46.6).

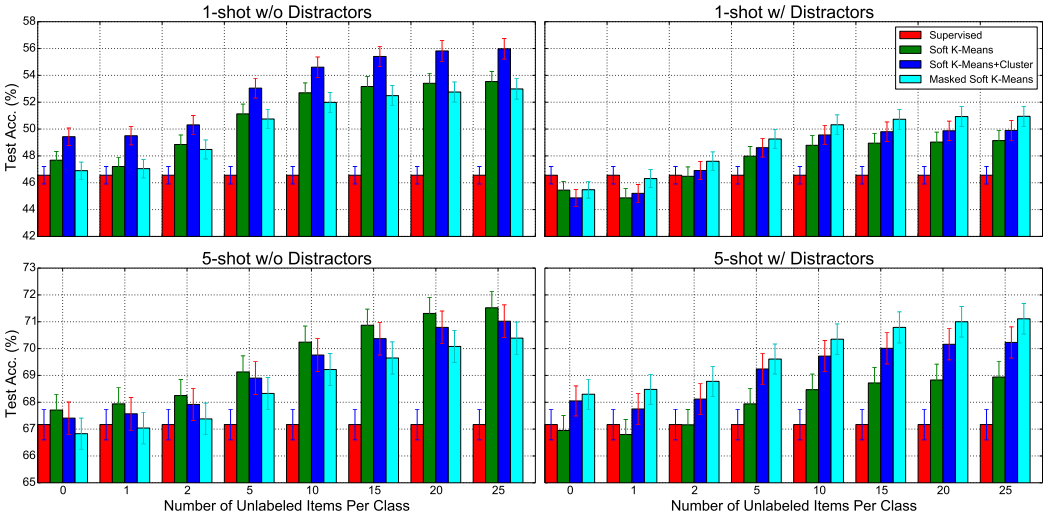

Figure 3: Model Performance on *tiered*ImageNet with different number of unlabeled items during test time.

4 Conclusion

In this work, we propose a novel semi-supervised few-shot learning paradigm, where an unlabeled set is added to each episode. We also extend the setup to more realistic situations where the unlabeled set has classes not belonging to the labeled classes. We also introduce a larger dataset split, *tiered*ImageNet, with hierarchical levels of labels. We propose several novel extensions of Prototypical Networks, and they show consistent improvements under semi-supervised settings compared to our baselines. As future work, we are working on incorporating fast weights [12, 6] into our framework so that examples can have different embedding representation given the contents in the episode.

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A *tiered*Imagenet Dataset Details

Each high-level category in *tiered*ImageNet contains between 10 and 30 ILSVRC-12 classes (17.8 on average). In the ImageNet hierarchy, some classes have multiple parent nodes. Therefore, classes belonging to more than one category were removed from the dataset to ensure separation between training and test categories. Test categories were chosen to reflect various levels of separation between training and test classes. Some test categories (such as "working dog") are fairly similar to training categories, whereas others (such as "geological formation") are quite different. The list of categories is shown below and statistics of the dataset can be found in Table 3. A visualization of the categories according to the ImageNet hierarchy is shown in Figure 4. The full list of classes per category will also be made public, however for the sake of brevity we do not include it here.

Table 3: Statistics of the *tiered*ImageNet dataset.

	Train	Val	Test	Total
Categories	20	6	8	34
Classes	351	97	160	608
Images	448,695	124,261	206,209	779,165

Train Categories: `n02087551` (hound, hound dog), `n02092468` (terrier), `n02120997` (feline, felid), `n02370806` (ungulate, hoofed mammal), `n02469914` (primate), `n01726692` (snake, serpent, ophidian), `n01674216` (saurian), `n01524359` (passerine, passeriform bird), `n01844917` (aquatic bird), `n04081844` (restraint, constraint), `n03574816` (instrument), `n03800933` (musical instrument, instrument), `n03125870` (craft), `n04451818` (tool), `n03414162` (game equipment), `n03278248` (electronic equipment), `n03419014` (garment), `n03297735` (establishment), `n02913152` (building, edifice), `n04014297` (protective covering, protective cover, protection).

Validation Categories: `n02098550` (sporting dog, gun dog), `n03257877` (durables, durable goods, consumer durables), `n03405265` (furnishing), `n03699975` (machine), `n03738472` (mechanism), `n03791235` (motor vehicle, automotive vehicle),

Test Categories: `n02103406` (working dog), `n01473806` (aquatic vertebrate), `n02159955` (insect), `n04531098` (vessel), `n03839993` (obstruction, obstructor, obstructer, impediment, impedimenta), `n09287968` (geological formation, formation), `n00020090` (substance), `n15046900` (solid).

B Extra Experimental Results

Figure 5 shows test accuracy values with different number of unlabeled items during test time. We observe clear improvement in test accuracy when the number grows from 0 to 25. Note that our models were trained with $M = 5$ and thus are showing an ability to extrapolate in generalization.

This confirms that, through meta-training, the models learned to acquire a better representation that will be more helpful after semi-supervised refinement. Figure 6 shows our mask output value distribution of the masked soft k-means model on Omniglot. The mask values have a bi-modal distribution, corresponding to distractor and non-distractor items.

C Hyperparameter Details

For Omniglot, we adopted the best hyperparameter settings found for ordinary Prototypical Networks in [4]. In these settings, the learning rate was set to 1e-3, and cut in half every 2K updates starting at update 2K. We trained for a total of 20K updates. For *mini*Imagenet and *tiered*ImageNet, we trained with a starting learning rate of 1e-3, which we also decayed. We started the decay after 25K updates, and every 25K updates thereafter we cut it in half. We trained for a total of 200K updates. We used ADAM [13] for the optimization of our models. For the MLP used in the Masked Soft k-Means model, we use a single hidden layer with 20 hidden units with a tanh non-linearity for all 3 datasets. We did not tune the hyparameters of this MLP so better performance may be attained with a more rigorous hyperparameter search.

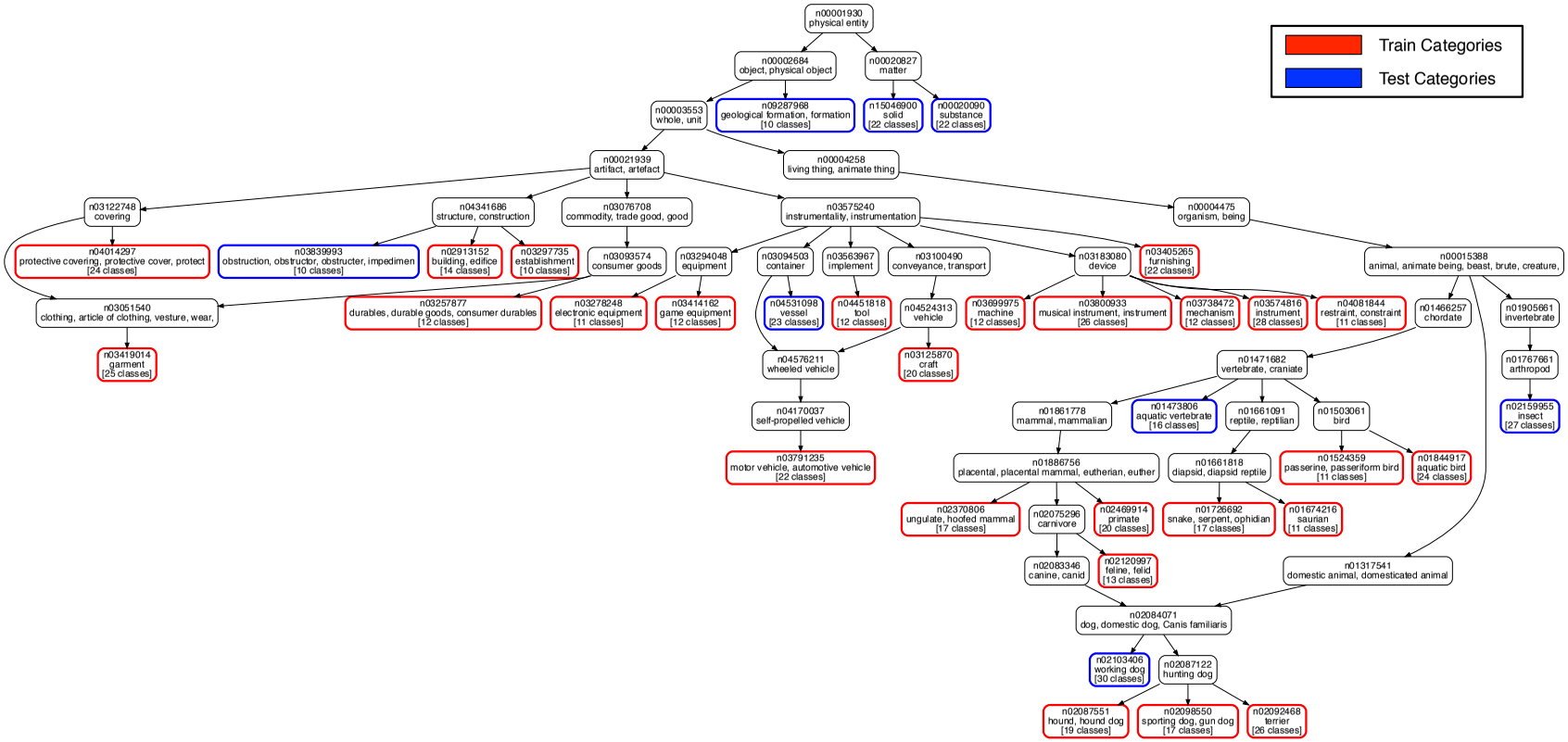

Figure 4: Hierarchy of *tiered*Imagenet categories. Training categories are highlighted in red and test categories in blue. Each category indicates the number of associated classes from ILSVRC-12. Best viewed zoomed-in on electronic version.

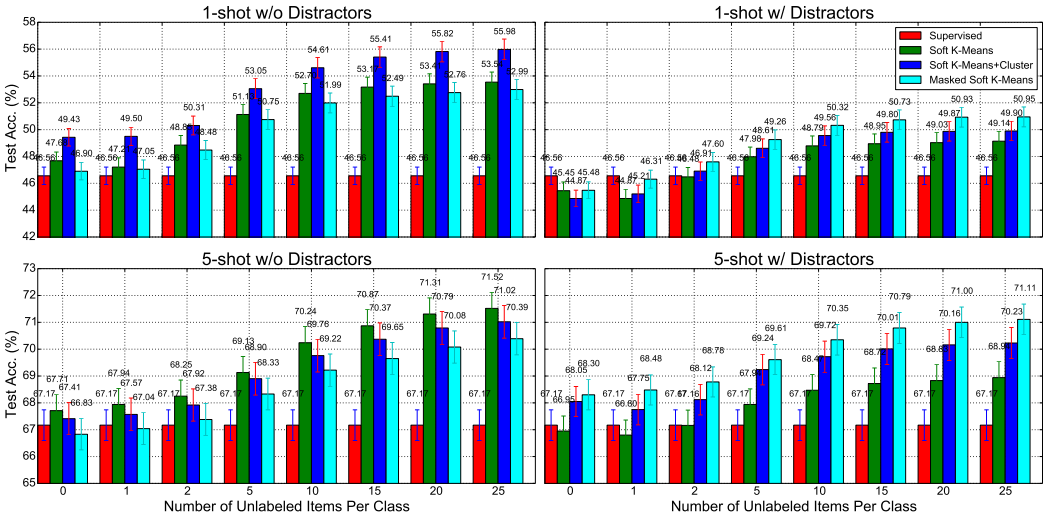

Figure 5: Model Performance on *tiered*ImageNet with different number of unlabeled items during test time. We include test accuracy numbers in this chart.

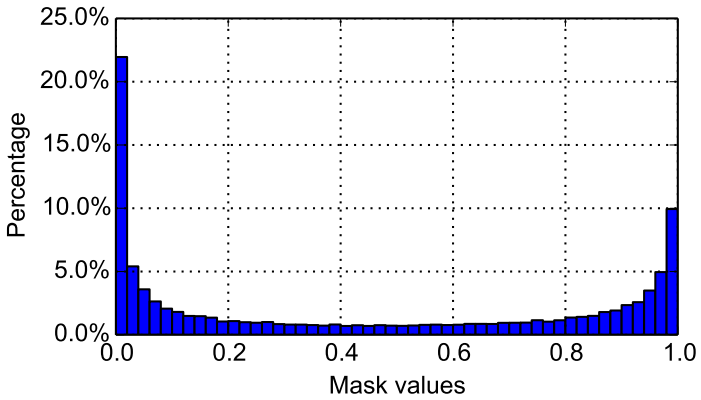

Figure 6: Mask values predicted by masked soft k-means on Omniglot.